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Advertising and Brand Attitudes: Evidence from 575 Brands over Five Years

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Report Summary

The ultimate goal of advertising is to influence sales. However, recent literature shows that it is very difficult to estimate advertising effectiveness on sales. Extremely large sample sizes are required to adequately power advertising experiments and observational methods may be a poor substitute for experimental estimates. Sales data are sparse and highly variable, ad effects tend to be small and short-lived, and advertising exposures are nonrandomly assigned.

Rex Yuxing Du, Mingyu Joo, and Kenneth Wilbur investigate whether brand attitudes can be reliable measures of advertising effectiveness. In contrast with sales data, brand attitude data are non-sparse and relatively stable, possibly more influenced by advertising (though most of the effect signs and magnitudes remain unknown), and measurable in large samples of consumers whose selection is unrelated to advertising treatment.

They examine a unique dataset of 575 established brands from 37 industries over a five-year observation window, merging weekly brand attitude survey data with weekly advertising expenditure data. In totality, the data include \$264 billion spent on advertising, 37% of all ad spend measured during the observation window, and approximately ten million brand attitude surveys.

They address the following three questions for mature brands that advertise regularly:

- How do brand attitudes change with advertising by the same brand and its competitors?
- How do these relationships vary across attitude measures and types of advertising media?
- How do various strategies to control for time-varying unobservables change effect sizes and precision?

The brand attitude metrics they consider are the percentages of survey respondents indicating favorable perceived quality, perceived value, and recent satisfaction for each brand in each week. The three types of advertising media they consider are national traditional media, local traditional media, and digital media. The models they estimate all include lagged brand attitudes, contemporaneous and lagged ad spending by type of media, brand fixed effects, week fixed effects, and weighted standard errors to reflect exogenous variation in the number of survey respondents each week.

They investigate two sets of control variables as partial remedies to this advertising timing endogeneity problem: brand/quarter fixed effects; and industry/week fixed effects. The data indicate that brand/quarter and industry/week fixed effects are individually and jointly important determinants of brand attitude data.

The key findings are that

- brand attitude metrics all rise with multiple lags of the brand's own national traditional advertising;
- local traditional ads increase perceived quality and perceived value;
- digital ads increase perceived value;
- the effects of competitors' ads are generally negative.

The results indicate that inclusion of proper control variables brings advertising parameter estimates closer to expectations without major reductions in estimation precision. However, the brand attitude data analyzed in this study provide insufficient power to estimate precise industry-specific effects, suggesting further investigation of other intermediate metrics such as store traffic, consideration, or information acquisition via online search as candidate advertising response measures.

Put into Practice

These findings and empirical strategies may aid marketers and their agencies in using data to guide important practical questions such as whether to advertise, how much to spend, and how to allocate ad budgets. Such empirical guidance may be especially needed in industries where available data complicate the estimation of causal effects of ads on sales, such as markets with long purchase cycles or long interpurchase times.

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1 Introduction

Advertisers seek to influence sales. Yet recent literature has called into serious question firms' ability to estimate how advertising influences sales. Consider two recent, prominent papers which rely on the "gold standard" of causal inference: randomized, controlled trials (RCTs).

Lewis and Rao (2015) reported the results of 25 advertising RCTs run on Yahoo.com, with an average of 1.3 million consumers per experiment. Despite these large sample sizes, most of the experiments were insufficiently powered to estimate positive advertising effects. Authors concluded that "we are making the admittedly strong claim that most advertisers do not, and indeed some cannot, know the effectiveness of their advertising spend."

Gordon et al. (2017) reported 15 advertising RCTs run on Facebook. With a total sample size of more than 500 million consumers, they were able to identify and precisely estimate positive treatment effects on sales. The main focus of the paper was to assess whether (non-experimental) observational methods such as matching and regression could recover causal effects of online advertising. The answer, broadly, was no, even when relying on extensive demographic and behavioral control variables.

From these two papers, we may conclude that extremely large sample sizes are required to adequately power advertising experiments and that observational methods may be a poor substitute for experimental estimates. The underlying reasons are that (i) sales data are sparse and highly variable, (ii) ad effects tend to be small and short-lived, and (iii) advertising exposures are nonrandomly assigned.¹

The purpose of the current paper, broadly, is to investigate whether brand attitude data can be reliably linked to advertising expenditures. In contrast with sales data, brand attitude data are (i) non-sparse and relatively stable, (ii) possibly more influenced by advertising, though most of the effect signs and magnitudes remain unknown, and (iii) measurable in large samples of consumers whose selection is unrelated to advertising treatment. Many large brands have subscribed to "brand tracking" surveys for decades, and the supply of such data may be increasing. For example, Facebook and Google both recently introduced products to estimate "lifts"

¹One might expect advertisers to frequently run highly powered RCTs, yet there is scant evidence of such practices (Rao and Simonov 2018).

in brand attitudes resulting from advertising.

This purpose is important for two primary reasons. First, the recent experimental evidence is limited to digital advertising. Digital advertising delivery facilitates experimentation and the measurement of individual-level response data, but the advertising medium is beset by several widespread problems that complicate experimental analysis, including ad (non-)viewability (IAB 2015), a high incidence of ad blocking by default (Shiller et al. 2018), non-human traffic (WhiteOps 2016), and advertising blindness (e.g., Owens et al. 2014).² Do conclusions drawn from digital advertising experiments also apply to traditional media? The question remains open, but previous literature offers mixed implications. For example, although some TV advertising experiments have exhibited low statistical power in split-cable designs (e.g., Lodish et al. 1995), quasi-experimental research on TV ads has estimated precise effects of advertising on sales and related behaviors (e.g., Du et al. 2017, Hartmann and Klapper 2018, Liaukonyte et al. 2015, Shapiro 2018, Tellis et al. 2000).

Second, although sales data are the most important indicator of advertising effects, they may not be the only, or even the best, statistical indicator of advertising response for all brands. Some firms – particularly those whose products exhibit long purchase cycles or long interpurchase times – may prefer to consider intermediate response variables such as brand attitudes. Consumers' brand attitudes are important indicators in their own right, as they reflect consumer perceptions about brand quality and value, and predict downstream behaviors such as search and consideration (Dotson et al. 2017). The financial value of brand attitudes are reflected in brand asset valuations; strong brands often sell for substantially more than physical asset valuations because consumer attitudes tend to persist, even when a brand changes owners. From a practical perspective, many advertisers cannot estimate causal effects of ads on sales, yet they still face operational questions such as whether to advertise; how much to spend; and how to allocate their expenditure across media. One possible way forward is to consider replacing sales data with other measures of consumer response to advertising.

More specifically, we address three primary questions. How do brand attitudes change with

²To be more specific, we suspect that ad viewability, ad blocking and ad blindness may produce large differences between intent-to-treat and average treatment effects; and non-human traffic may inflate true sample sizes.

advertising by the same brand and its competitors? How do these relationships vary across attitude measures and types of advertising media? How do various strategies to control for time-varying unobservables change effect sizes and precision? Our goal, to the extent possible, is to "let the data speak" by applying comparable methods to comparable measures for many advertising brands.

To answer these questions, we examine a unique dataset of 575 established brands from 37 industries over a five-year observation window, merging weekly brand attitude data with weekly advertising expenditure data. In totality, the data include \$264 billion spent on advertising, 37% of all ad spend measured during the observation window, and approximately ten million brand attitude surveys. We study mature brands that advertise regularly.

The brand attitude metrics we consider are the percentages of survey respondents indicating favorable perceived quality, perceived value and recent satisfaction for each brand in each week. The three types of advertising media we consider are national traditional media, local traditional media, and digital media. We suspect that each type of advertising could operate directly on each brand attitude: advertising content may communicate differentiating features, thereby influencing perceived quality; it could communicate current pricing terms, thereby influencing perceived value; and it could lead a consumer directly to purchase, thereby increasing the proportion of people who indicate recent satisfaction. Although we believe that any of these effects may operate, we expect perceived quality to be most strongly linked to national advertising, as national ads typically convey product information and differentiating messages (Liaukonyte et al. 2015). We expect perceived value to rise more strongly with local traditional advertising and digital advertising, as pricing and availability frequently vary geographically and such information is often communicated via advertising in geographically targeted media (Kaul and Wittink 1995, Lee et al. 2017, Xu et al. 2014).

The models we estimate all include lagged brand attitudes, contemporaneous and lagged ad spending by type of media, brand fixed effects, week fixed effects, and weighted standard errors to reflect exogenous variation in the number of survey respondents each week. The fundamental challenge to causal inference in this setting is not in the nonrandom assignment of advertisements to consumers; brand attitude data are collected from large samples of consumers

whose selection is unrelated to advertising efforts. Instead, there is a primary difficulty in the *timing* of advertising expenditure, as advertising timing may be nonrandomly selected and could coincide with periods of peak demand or heightened responsiveness to advertising.

We investigate two sets of control variables as partial remedies to this advertising timing endogeneity problem: brand/quarter fixed effects, to control for time-varying, brand-related unobservables that may drive both advertising and brand attitudes; and industry/week fixed effects, to control for industry-level unobservables that may affect multiple competing brands' advertising and brand attitudes. When both sets of control variables are included, causal interpretation requires an assumption that advertising expenditures are not chosen with knowledge of future brand/week departures from brand/quarter unobservables or future brand/week departures from industry/week unobservables. Although this identifying assumption is unlikely to apply to every brand, we suspect it applies to the large majority of brands in the sample.

To summarize the primary findings, the data indicate that brand/quarter and industry/week fixed effects are individually and jointly important determinants of brand attitude data. Further, the model that includes both sets of control variables produces results that comport better with expectations, and exhibit greater internal coherence, than a descriptive model without either set of control variables. The estimates indicate that (i) brand attitude metrics all rise with multiple lags of the brand's own national traditional advertising; (ii) local traditional ads increase perceived quality and perceived value; (iii) digital ads increase perceived value; (iv) the effects of competitors' ads are generally negative.

Next, we discuss how the current study relates to extant literature. The subsequent sections explain the data and provide some model-free evidence; discuss identification issues; specify the empirical models; report and interpret the findings; and discuss the overall learnings, limitations and implications of the exercise.

1.1 Relationship to Previous Literature

The empirical literature on advertising is vast. Most relevant is the set of papers that demonstrates that advertising can affect intermediate consumer outcomes, i.e., behaviors and attitudes that occur prior to sales. For example, Draganska and Klapper (2011) show that advertising

increases brand awareness and expands consumer choice sets; Joo et al. (2014) found that TV advertising increases the number of product category-related Google searches and the proportion of searches that contain brand-specific keywords; and Hu et al. (2014) show that advertising predicts monthly search for automotive brands, which in turn predicts monthly purchase data. There are also several papers that estimate industry-specific correlations between brand attitudes and advertising expenditures (Hanssens et al. 2014, Srinivasan et al. 2010).

The most closely related paper is Clark, Doraszelski, and Draganska (2009), which estimated advertising effects on brand awareness and perceived quality in a large annual panel dataset, including \$96B in ad spending by 348 brands from 2000-2005. As that paper explains, most of the prior literature was based on cross-sectional data, with questionable ability to separate effects of advertising from unobserved confounds such as product quality. Clark et al. (2009) found, in their preferred specification, that a focal brand's own advertising increased its own awareness but did not significantly change perceived quality. The focal brand's competitor advertising, by contrast, reduced brand awareness and increased perceived quality. Although the current analysis replicates some aspects of Clark et al. (2009), our incremental contribution rests on several important differences: temporal disaggregation, methods, measures and results.

The most important difference may be the temporal dimension of the data. Clark et al. (2009) analyzed a "large-N, small-T" type panel with 4.2 observations available for the average brand. The current paper, by contrast, investigates a balanced panel of 575 brands over 252 weeks of data, consistent with the central findings of Tellis and Franses (2006) that "too disaggregate data does not cause any disaggregation bias." More granular data allow for more extensive controls for possible time-varying confounds, one of the central themes of our paper. In fact, Clark et al. (2009, p. 229) said "Perhaps the ideal data for analyzing the effect of advertising are time series of advertising expenditures, brand awareness, and perceived quality for the brands being studied. With long enough time series we could then try to identify for each brand in isolation the effect of advertising expenditures on brand awareness and perceived quality." Intuitively, the more disaggregated data allows for a sharper delineation of the lead/lag relationships between the timing of ad spend (which is highly variable over time) and brand attitudes (which mostly exhibit stable long-run averages). There is further interest in contrasting results based on their

2000-2005 sample period with the later time period of 2008-2012, as consumer media habits and firm ad spending changed significantly between these two time periods; for example, digital advertising increased substantially.

There are also important differences in attitude measures, methods and results. Clark et al. (2009) observed average ratings of perceived quality on a 0-10 scale, and defined awareness as the percentage of respondents who rated the brand's quality. The metrics studied in this paper indicate multiple dimensions of brand attitudes, including one (recent satisfaction) which may reflect recent purchase activity; but they do not explicitly separate awareness from other attitudes. We further distinguish between the effects of three types of ad spend (national traditional, local traditional and digital). Clark et al. (2009) relied on dynamic panel instrumental variables estimators to control for advertising endogeneity, with findings that differed qualitatively across estimators. The exogeneity conditions require knowledge about the serial correlation of the error terms, information which is difficult to derive from theory or test in "small-T" settings. Finally, the empirical findings differ substantially: we find positive effects of own ad spend on perceived quality; we offer the first findings related to perceived value, recent satisfaction and individual types of advertising; and we find that competitor ad spending generally decreases brand attitudes.

The current study is further related to a set of papers comparing advertising effects across media and across competitors. For example, Danaher and Dagger (2013) offered an approach to help brands evaluate relative media effectiveness by linking loyalty program members' purchases to their responses on a media consumption survey. Draganska et al. (2014) showed that television advertisements produced statistically indistinguishable "lift" in aided brand recall to three formats of online advertisements (video, banner and rich media); but proper inference depends critically on accounting for differences in pre-existing brand knowledge between people exposed to different ad formats. Lovett et al. (2017) investigated a large panel of brands, showing that internet and television ad spend both have small but significant positive effects on word-of-mouth. There is also evidence that competitor advertising can interfere with advertisement recall (Kent and Allen 1994) and sales response (Danaher et al. 2008).

More broadly, the current study relates to the literature that estimates advertising effects on

brand equity. Ailawadi et al. (2003) introduced estimation of customer-based brand equity and reported a positive association between advertising and brand equity. Borkovsky et al. (2017) found that advertising investment increases the expected net present value of future cash flows due to a brand in a dynamic model of advertising investment. Mela et al. (1997) found that advertising makes consumers less price sensitive and reduces the size of the non-loyal segment. Our results offer evidence consistent with possible attitude-related mechanisms underlying these important findings.

2 Data and Model-free Evidence

Two large-scale commercial databases are combined – brand attitude survey data from YouGov and ad spending data from Kantar. We believe both data sources to be "best in class." Both Kantar and YouGov are leading market research agencies.³ To the best of our knowledge, there are no data sources that provide both better quality and similar coverage. We further believe that these two databases are the market leaders in their product categories, suggesting that we are using similar data to what many practitioners have available. However, the data do have some nuances that are important to consider when interpreting the results of the analysis. We first describe the data sources and focal metrics, then the sample selection, followed by summary statistics and model-free evidence.

2.1 Brand Tracking Data

Brands employ market research firms to conduct longitudinal surveys to monitor consumers' brand attitudes. Although such surveys have traditionally been quite costly, there are numerous research agencies that offer similar products, including GfK, Millward Brown, TNS and YouGov. Recently, Facebook introduced its own survey platform to enable brands to "accurately measure brand awareness, impact and ad recall." The weaknesses of survey data are numerous and well documented. However, regular surveys of large consumer panels produce brand attitude data that are reasonably stable over time, although individual data points can be affected by sampling

³https://www.ama.org/publications/MarketingNews/Documents/2017-top-50-gold-report-article.pdf, accessed March 2018.

⁴https://www.facebook.com/business/learn/facebook-brand-polling, accessed March 2018.

error. When meaningful changes do occur, they often correspond to identifiable shocks, such as news events or quality changes.

Brand tracking data were drawn from the largest available survey panel, the YouGov BrandIndex. YouGov maintains a panel of more than 1.5 million U.S. consumers, with each panelist invited to complete up to one survey online each month. Panelists are compensated with redeemable "points" each time they complete a survey, but survey participation is not mandatory, leading to some exogenous fluctuations in the number of surveys completed for each industry in each week.

Each survey respondent was asked one of seven attitude questions about seven different industries, with a different question for each industry. The standardized response format, depicted in Figure 1, solicited responses for 25-40 brands within each industry. The survey instrument asked, for example, "Which of the following broadcast and cable networks do you think represents good quality?" and then lists thirty television networks in random order. The respondent could mark as many brands as desired with no time limit, suggesting that the data should reflect absolute levels of quality, as perceived by the respondent.

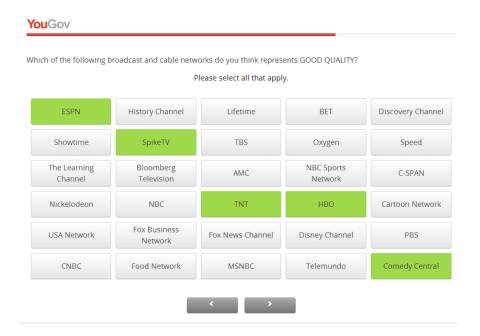
YouGov collected data using the following set of questions:

- "Which of the brands do you associate with good quality?"
- "Which of the brands do you associate with good value-for-money?"
- "Would you identify yourself as a recent satisfied customer of any of these brands?"
- "Which brands would you recommend to a friend?"
- "For which brands do you have a 'generally positive' feeling?"
- "Which of the brands would you be proud to work for?"
- "Over the past two weeks, which of the following brands have you heard something positive about (whether in the news, through advertising, or talking to friends and family)?"

The survey items remained constant throughout the sample period.

YouGov uses respondent demographics to weight the data and construct nationally representative averages. The brand attitude data estimate the weekly percentage of U.S. consumers

Figure 1: Survey Instrument Example



that would provide a positive response to each of these seven questions for each brand, and further indicate the weekly number of respondents answering each question for each industry.

An important limitation of the brand attitude data is that some level of awareness is presumably required to provide a positive indication for a brand. For example, in Figure 1, a respondent who has never heard of the Speed network will presumably not indicate that the network represents good quality. We view this as a regrettable but reasonable limitation of the brand attitude data. Some level of consumer awareness or familiarity is a prerequisite to the brand attitudes that we are able to observe.

We focus our study on the metrics of perceived quality, perceived value and recent satisfaction. Perceived quality and perceived value both relate to identifiable messages that are frequently communicated through advertising, such as differentiating statements about product attributes or current pricing terms. Recent satisfaction is the brand attitude metric that comes closest to indicating sales; if advertising increases sales, then it should also lift the proprotion of consumers who indicate that they are recently satisfied customers of the brand.

2.2 Advertising Expenditure Data

Kantar Media compiles comprehensive data on advertising placements and expenditure estimates across the broad range of advertising media listed in Table 1. Kantar is widely viewed as the market leader in "competitive advertising intelligence," i.e., the service of monitoring competitors' advertisement placements and expenditures.

Kantar tracks television, print and digital media by logging brand advertisement insertions algorithmically through continuous monitoring of media content. For television and print media, estimated advertising prices are provided by media outlets indirectly through the Standard Rate and Data Service (SRDS). Although the SRDS price estimates are known to be imperfect, they are commonly used by brands to plan future advertising efforts, and are the only available source of widespread information about advertising prices.⁵ Digital advertising placements are collected by an elaborate system of web crawlers. Outdoor and radio ad placements and prices, and digital advertising price data, are provided directly to Kantar by industry partners.

We paid particular attention to Kantar's data quality in internet display and internet search data, as these measures were relatively new at the time we collected the data. The internet search ad spend data did not appear reliable: they were unreasonably sparse. Our investigations of internet display data did not indicate any identifiable problems. Therefore our measure of digital advertising includes internet display media only. We remain cognizant of the possibility of classical errors-in-variables problems which may bias parameter estimates toward zero and bias t-statistics downward (Griliches 1977), thereby yielding false null results. However, we do find significant effects of own digital and competitor digital advertising on brand attitudes.

Advertising content varies by type of media. National traditional ads are often used to communicate information and differentiating messages (Liaukonyte et al. 2015), while local traditional ads focus more on current price and availability, as these variables typically vary across local markets, while also conveying some quality-relevant information (Kaul and Wittink 1995). Digital advertising also frequently communicates current pricing and availability. For

⁵The reporting incentives are mixed. A media outlet could exaggerate its ad price to offer perceived discounts in negotiations with advertisers. Or, a media outlet might underreport its ad price to attract interested advertisers. Actual ad prices in traditional media are typically set in confidential bilateral negotiations and may reflect price discrimination or quantity discounts. Digital advertising prices are typically set in complex, rapidly changing spot auction markets within or between ad networks, demand-side platforms and supply-side platforms.

Table 1: Advertising Media Tracked in Stradegy Database

National Media	Local Media	Digital Media
Business-to-Business	Local Magazines	Internet Display
Cable TV	Local Newspapers	Internet Search
National Newspapers	Hispanic Newspapers	
Magazines	Sunday Magazines	
Hispanic Magazines	Spot TV	
National Spot Radio	Syndicated TV	
Network Radio	Local Radio	
Network TV	Outdoor	
Spanish Language TV		

example, Lee et al. (2017) quantified the contents of 100,000 Facebook ads. They reported that 62% of ads offered deals ("discounts or freebies"), 44% compared prices, and 69% contained information on where to obtain a product. Yang et al. (2015) quantified search advertisement content for hotels, travel intermediaries and auto manufacturers, finding that they used 14%, 25% and 6% of space, respectively, to communicate pricing terms.

Local traditional ads offer better targeting than national traditional ads, as they may vary across geographic markets. Digital ads can be even better targeted, based on demographic and behavioral variables, as well as geographically. A few recent studies have found that banner advertisements can increase sales (e.g., Lewis and Reiley 2014), internet video ads have been found to be as effective as TV ads in brand building (Draganska, Hartmann, and Stanglein 2014), and digital advertising revenues have grown much faster than traditional advertising in recent years. On the other hand, some published research has called digital ad effectiveness into serious question (Blake et al. 2015, Lewis and Rao 2015); digital ads are subject to higher levels of ad non-viewability, passive ad blocking, ad blindness and non-human traffic; and some prominent brands including GM and P&G have publicly questioned whether digital campaigns are cost-effective.⁶

The differences in advertising content and targeting across categories of advertising media

 $^{^6}$ https://www.wsj.com/articles/SB10001424052702304192704577406394017764460, https://www.wsj.com/articles/p-g-cuts-more-than-100-million-in-largely-ineffective-digital-ads-1501191104, accessed March 2018.

lead us to suspect that relationships between brand attitudes and advertising expenditures may vary across these three categories of advertising media.

2.3 Sample Selection

The goal of this study is to estimate relationships between advertising expenditures and brand attitudes for mature brands that advertise regularly. We select brands with these particular criteria in mind, so we begin with the acknowledgement that the results can only be interpreted as applicable to the set of brands studied and may not generalize beyond that set. Although this strategy does not represent the full population of brands, this subset is large and particularly important, as it accounted for 37% of all advertising expenditure measured during the sample period.

We first matched each brand in the YouGov data to its equivalent entity in the Kantar database. We then downloaded weekly ad spend data for each brand in each equivalent time period. Finally, we retained brands that (a) were tracked by YouGov for the entire sample period, (b) advertised in at least 30% of the observed weeks, and (c) did not go more than thirteen consecutive weeks with zero advertising. The set of 575 brands meeting these criteria is provided in the appendix, along with each brand's industry as indicated by YouGov. In total, these brands spent \$264 billion on advertising from 2008-2012, or \$92 million per brand per year. The corresponding brand attitude metrics are based on about ten million surveys, yielding a weekly average of 595 responses per question per brand (SD=77).

2.4 Descriptive Statistics and Model-free Evidence

We first summarize the brand attitude data, followed by the ad spend data. We then visualize the relationships between them for a few selected brands, then present quantiles of brand-level correlations between the key variables in the analysis.

Figure 2 shows how the average brand attitude metric (perceived quality, perceived value and recent satisfaction) changed for each industry in each year of the sample. The highest rated industries were consumer goods, tools/hardware and soft drinks; banking, prescription drugs, grocery retailing, casinos and financial service industries rank near the bottom. Some

of these industry-level differences are partially driven by brand awareness, as large consumer goods brands are available throughout the U.S., whereas many brands in some of the lower-rated industries are more geographically dispersed (e.g., grocery retailers, consumer banks). Consumers in unserved regions would not indicate positive attitudes toward brands they have not encountered, as awareness must precede perceived quality, perceived value or recent satisfaction.

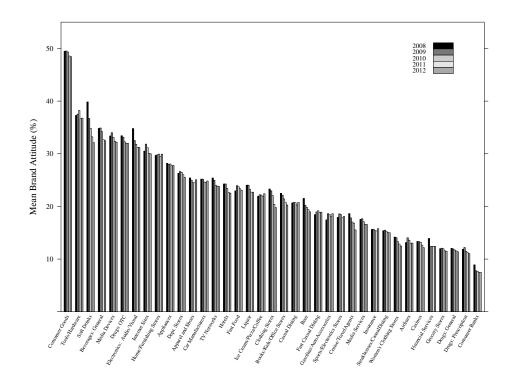


Figure 2: Brand Attitudes by Industry and Year

The industry-level averages of brand attitude metrics are fairly stable across years in the sample, with a few exceptions. For example, consumer perceptions of soft drinks slipped sharply during the sample period. There is also a general negative trend in audio/visual electronics, though this shift in averages masks heterogeneity and consolidation; a few newer brands like LG and Acer improved, whereas some older brands (e.g., Kodak, Sony, Panasonic) fell. Despite these few exceptions, the industry-year averages were mostly stable during the sample period.

Table 2 provides further information about how brand attitudes changed across years of the sample. Across all brands, perceived quality fell by an average of 1.6% between 2008 and 2012; perceived value fell by 0.3% and recent satisfaction fell by 0.9%. These trends speak to the

importance of controlling for time-varying unobservables in estimating relationships between ad spend and brand attitudes.

Table 2: Mean Brand Attitudes

	Perceive	d Quality	Perceive	ed Value	Recent Satisfaction				
	In 2008	In 2012	In 2008	In 2012	In 2008	In 2012			
Mean	26.5%	24.9%	20.6%	20.3%	20.2%	19.3%			
Median	24.4%	22.8%	17.4%	17.1%	15.9%	15.0%			

Next, we summarize the ad spend data. Figure 3 displays mean brand ad spend by industry and year. Media and automotive brands spent the most on advertising, followed by department store, insurance and quick service restaurant brands. Except for a few notable exceptions (e.g., media, department stores, insurance), most industries did not exhibit large changes in mean brand ad spend between 2008 and 2012.

Figure 3: Ad Spending by Industry and Year

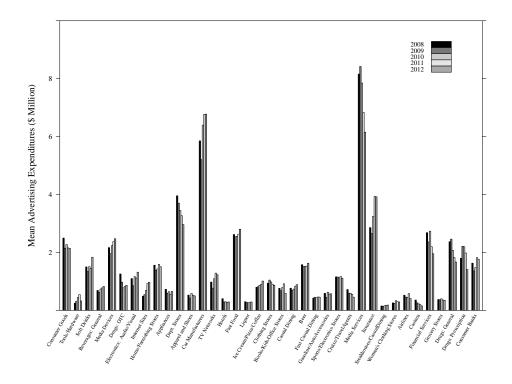


Table 3 summarizes brand-level changes in ad spend by type of media between 2008 and 2012. There was some consolidation in national traditional ad spending during the sample,

as the average brand's weekly expenditure rose by about \$50,000, whereas the median brand's weekly ad spend fell by \$22,000. Local traditional advertising fell substantially during the sample, with the average brand spending 25% less per week in 2012 relative to 2008. Digital ads rose from \$110,000 per brand per week in 2008 to \$130,000 in 2012.

Table 3: Mean Advertising Expenditure (\$ Millions)

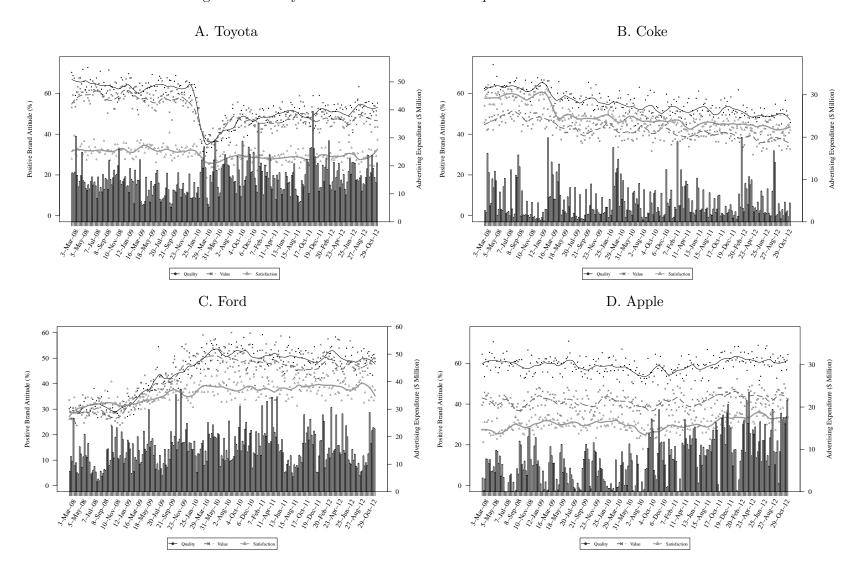
	National	Trad. Ads	Local Tr	ad. Ads	Digital Ads			
	In 2008	In 2012	In 2008	In 2012	In 2008	In 2012		
Mean	\$1.02	\$1.07	\$0.51	\$0.38	\$0.11	\$0.13		
Median	\$0.27	\$0.25	\$0.11	\$0.09	\$0.01	\$0.02		

Next, we focus on a series of visualizations for selected brands. Panel A of Figure 4 presents the three brand attitude metrics for Toyota along with the brand's weekly ad spend data. The dots represent brand attitude data points in each week whereas the trend lines are generated by local regression. Toyota's quality and value perceptions held steady at about 60% until 2009, then dropped sharply to 30% in 2010, due to a highly-publicized series of auto recall and safety incidents. They later began a slow recovery, though not quite up to the previous level. Unlike quality and value, recent satisfaction started out far lower around 30%, and was less affected by the recall. Throughout this time period, advertising policy changed somewhat, but the peaks in ad spend do not correlate with immediate improvements in brand attitudes.

Panel B of Figure 4 presents similar data for Coke. Like the aggregate trend of soft drinks in Figure 2, and industry-level consumption figures more generally, respondents' attitudes toward Coke's perceived quality, perceived value, and recent satisfaction show gradual downward slopes which added up to a meaningful slide from 63% to 50% in perceived quality from 2008-2012. Although ad spend varies substantially throughout the sample, there is little visual evidence of any correspondence between brand attitudes and advertising expenditure.

Ford's brand attitude metrics, in Panel C, show a greater divergence than most brands. Quality and value perceptions increased early in the sample before leveling off around 50%. Recent satisfaction initially approximated quality and value, but then leveled off at 40%. Again, ad spend is highly variable, but there is little or no visual evidence that the peaks and troughs correspond to changes in brand attitudes.

Figure 4: Weekly Brand Attitudes and Ad Expenditures of Selected Brands



Finally, Apple's brand attitudes (Panel D) were fairly stable throughout the sample period. However, the three attitude metrics differed substantially, as perceived quality (about 60%) was far higher than perceived value (about 40%), which in turn substantially exceeded recent satisfaction (about 30%). As in the other case studies, the brand's ad spend varied substantially, though it is again difficult to see a correspondence between advertising and brand attitudes.

Several aspects of these four case studies replicate broadly throughout the sample. First, weekly brand attitude data generally vary around stable long-run averages. For this reason, we will use the number of survey respondents in each brand/week/metric observation to differentially weight observations according to how informative each observation is. Second, ad spend data are highly variable across weeks within each advertiser/quarter, though annual totals of advertising spend typically do not change much. Third, the relationship between advertising expenditure and brand attitudes is difficult to discern visually, even across long time horizons, motivating an econometric modeling approach to isolate the effects of advertising from possible confounding variables. Fourth, non-advertising events (such as the Toyota product harm crisis) may change brand attitudes significantly, suggesting a substantial importance of controlling for such confounds in a modeling framework.

Finally, we use the 252 weeks of data to construct brand-level correlations among the key variables. Table 4 presents the medians and central 90% ranges of the brand-level correlations. Overall, brand attitude metrics are positively correlated with each other for most brands, with median correlations ranging from .10-.13. Among the ad spend variables, national and local traditional advertising are the most highly correlated (median of .24) whereas digital is weakly correlated with each (median .06 with national, .04 with local). Finally, confirming what we saw in the four brand case studies, the median correlations between brand attitudes and ad spend measures are all near zero, ranging from .00 (digital/satisfaction) to .03 (national/quality and national/value).

Table 4: 5th, 50th, and 95th Percentiles among Brand-level Correlations

	Perceived Quality	Perceived Value	Recent Sat.	Nat'l Trad.	Local Trad.	Digital
Perceived Quality	1					
Perceived Value	[04, .12, .49]	1				
Recent Satisfaction	[04, .13, .51]	[06, .10, .47]	1			
National Trad.	[14, .03, .22]	[12, .03, .22]	[13, .02, .20]	1		
Local Trad.	[15, .01, .20]	[14, .02, .16]	[14, .01, .18]	[05, .24, .62]	1	
Digital	[19, .01, .19]	[14, .01, .18]	[16, .00, .18]	[09, .06, .38]	[10, .04, .33]	1

3 Endogeneity, Identifying Assumptions and Control Variables

Numerous measurement and endogeneity problems arise in advertising response estimation. Traditional mass media advertisements are simultaneously transmitted to many people, either at the national or local level. Firms can often obtain noisy estimates of ad reach, and they can often directly measure or estimate the number of conversions (e.g. store visits, sales, leads accrued) that occurred after the message was transmitted. However, in the case of traditional advertising, they typically cannot link advertisement exposure with conversions at the individual level, as is often possible in digital advertising. In both traditional and digital advertising, it is difficult to separate advertising treatment effects from strategic targeting policies. In all cases, the fundamental difficulty is in determining what conversions would have occurred had the advertising not taken place. Estimation of weak advertising effects in statistically noisy environments is further complicated by frequent consumer disregard or avoidance of advertisements; repeated exposures and possibly nonlinear effects of ads on sales; frequent misattribution of advertised messages to competing brands, and other forms of competitive advertising interference; and advertisement copy rotation, "wear-out" and time-varying message effectiveness.

We are aware of three prominent research designs to estimate quasi-experimental advertising effects in traditional media. Each exploits particular institutional details:

• Hartmann and Klapper (2018) rely on local variation in regional preferences for watching featured sports teams, along with the simultaneous carriage of national ads in all local markets, and the allocation of ad slots to advertisers before the competing teams are known, to estimate the impact of national Super Bowl ads on local beverage sales. Under these conditions, each local market has a quasi-random component of its viewership of

national ads, leading to exogenous variation in advertising exposures across local markets.

- Shapiro (2018) exploits discontinuities in local television advertising intensity that occur at edges of contiguous geographic television markets to identify the treatment effects of local TV advertising on county-level response variables. The quasi-experimental logic relies on the similarity of neighboring counties on opposite sides of local television market borders, leading to numerous observations of county pairs exposed to different intensities of advertising treatment. The approach can be applied to estimate the effect of local TV advertising on any response indicator observed at the county level.
- Liaukonyte et al. (2015) rely on quasi-random national TV advertisement insertion times to estimate effects on brand website traffic and sales. The treatment/control logic relies on examining narrow windows of time, such as two minutes immediately before the TV ad and two minutes after, along with typical TV industry practices of contractually unspecified commercial break start times and randomized advertisement ordering within commercial breaks. The treatment/control logic assumes that the observation windows are narrow enough that no competing explanations can plausibly account for changes in pre-ad and post-ad response variables.

Each of these research designs advances our ability to estimate causal advertising effects by applying quasi-experimental econometric techniques to retrospective field data, but each relies on specific institutional details. In particular, none of these strategies is able to answer the research questions that motivate the current analysis, as brand attitude data are only observed for the national market on a weekly basis for each brand.

In contrast to academic research, practitioners often identify advertising effects using an assumption of precedence.⁷ That is to say, if advertising preceded sales, then any discernible response of sales is attributed to the advertising that came before it. There are also some published studies of advertising effects that infer causality using a similar identifying assumption. The typical argument for the validity of this identification strategy is that a brand's ad spending must be determined prior to the firm's observation of the response variable.

⁷See, for example, http://pages.stern.nyu.edu/ãtakos/studentevents/3-28-12MeasuringROMISlideDeck.pdf or https://en.wikipedia.org/wiki/Marketing_mix_modeling, accessed March 2018.

One need not presume much sophistication on the part of a marketer to show that the precedence assumption can be tainted by unobserved variables. As a simple example, suppose that a brand knows that demand tends to rise in a promotion week, and that the brand prefers to advertise more heavily during periods of peak demand; then both sales and advertising could be simultaneously influenced by the third variable (promotion week), yielding a spurious or inflated finding of ad effects on sales. Similar arguments can be based on any number of unobserved variables—e.g., changes in wholesale or retail prices, distribution, product assortments and line extensions, trade promotions, competitor marketing mix variables—that may correlate with both advertising and sales.

Arguments against precedence need not depend on unobserved variables. For example, if the marketer correctly anticipated a likely future change in future revenues, and set ad spend as a proportion of anticipated future revenues, then ad effect estimates may be biased upward by simultaneity. The key problem is that the advertising policy function is unobserved by the econometrician and may depend on anticipation of future changes in the response variable.

Anecdotally, when we discuss such issues with practitioners, we find three typical reactions. One is an understanding and agreement that advertising response estimates are likely to be biased, coupled with a belief that biased estimates are likely better than no estimates at all. Another common response is a gap in understanding endogeneity issues: we rationalize this with the observation that most business schools did not start teaching causal methods until relatively recently; large brands have traditionally not screened their marketing recruits for this skill; and incentives to experiment may be distorted by the principal/agent relationships that are nearly ubiquitous in practice. The third common refrain is a deep skepticism that brand advertising decisions are made strategically. Executives in several organizations have told us that their company sets quarterly or annual advertising budgets and that the agencies allocate the budget across media programs and weeks without anticipation of likely changes in the market.⁸

Naturally, we are unable to characterize the full set of endogeneity problems for the 575 brands and 37 different industries represented in these data. Yet we would like to consider how

⁸We remain circumspect about this argument, as agencies may be aware of their clients' evaluation function and act to maximize their own incentives to demonstrate advertising effects to their clients.

various control strategies might influence estimates of advertising effects on brand attitudes in a broad sample of mature brands that advertise regularly. We consider four main specifications:

- Descriptive regression with multiple lags of brand advertising and competitor advertising, controlling for lagged response variables, brand effects, time effects and weighted standard errors.
- 2. Descriptive regression (1) with industry/year/week fixed effects added (we call these "industry/week" effects).
- 3. Descriptive regression (1) with brand/year/quarter fixed effects added (we call these "brand/quarter" effects).
- 4. Descriptive regression (1) with both industry/week and brand/quarter fixed effects added, 21,194 fixed effects in all.

The industry/week fixed effects should control for any industry-level unobservables in a given week that affect all brands' advertising expenditures, such as seasonal fluctuations in industry demand. There are many brands observed within every industry, providing sufficient variation to estimate a separate industry fixed effect for each week of the sample.

The brand/quarter fixed effects should control for any brand-level unobservables that persist across weeks within a quarter, such as budgetary changes or persistent changes in unobserved marketing variables. There are 13 weeks of brand attitude data within each quarter, yielding sufficient data to estimate a separate brand fixed effect for each quarter in the sample.

In the model that contains both industry/week and brand/quarter fixed effects, the assumption required for causal interpretation is that brand-week fluctuations of ad spending are uncorrelated with (i) brand-week departures from brand-quarter unobservables and (ii) brand-week departures from industry-week unobservables. Although still imperfect, this assumption is much weaker and more plausible than the typical assumption that advertising spend is uncorrelated with brand-week unobservables. We think this assumption is probably reasonable for most brands whose attitudes are largely stable across quarters, as is typical in the sample that we study. However, we acknowledge that the assumption may be violated, especially in the

presence of systematic weekly fluctuations in drivers of brand attitudes that can be anticipated by the brand and are used to set advertising policies.

Of course, what we would really like to control for is brand/week fixed effects, but these would covary perfectly with the advertising data and therefore would prevent estimation of the quantities of primary interest. Still, we believe that the two sets of control variables might, together, handle some common sources of endogeneity and let us offer, at minimum, a first approximation of the effects of ad spend on brand attitudes. We also think it might be instructive to observe how the control variables change the qualitative conclusions.

In sum, we try to control for time-varying confounds as much as possible, so the main model results can be interpreted as causal subject to a clearly specified identifying assumption. As we await highly powered RCTs in traditional media or more comprehensive quasi-experimental research designs, we hope that the estimates below may be viewed as suggestive of causal effects, subject to appropriate caveats, and possibly useful to marketers and their advertising agencies as they think about how to allocate advertising budgets and apply appropriate control variables in similar settings.

4 Models

The main goals of this paper are to estimate relationships between brand attitudes and ad spend variables; to show how these effects vary across types of advertising media; and to illustrate how control variables change the estimates. We seek to "let the data speak" by specifying simple models and contrasting the results across comparable metrics and control variables.

We represent the log of one plus any focal brand attitude metric for brand b in industry i in week t as y_{bt} and the other two metrics with y'_{bt} and y''_{bt} . The log of one plus national traditional, local traditional and digital ad spend for brand b in week t are na_{bt} , la_{bt} and da_{bt} , respectively; its competitors' log of one plus ad spend observed in week t are na^c_{bt} , la^c_{bt} , and da^c_{bt} in national, local and digital media, respectively.

The model specification is

$$y_{bt} = \sum_{\tau=1}^{T_y} \alpha_{\tau}^y y_{b,t-\tau} + \sum_{\tau=1}^{T_y} \alpha_{\tau}^{y'} y'_{b,t-\tau} + \sum_{\tau=1}^{T_y} \alpha_{\tau}^{y''} y''_{b,t-\tau}$$

$$+ \sum_{\tau=0}^{T_a} \beta_{\tau}^{ny} n a_{b,t-\tau} + \sum_{\tau=0}^{T_a} \beta_{\tau}^{ly} l a_{b,t-\tau} + \sum_{\tau=0}^{T_a} \beta_{\tau}^{dy} d a_{b,t-\tau}$$

$$+ \sum_{\tau=0}^{T_a} \beta_{\tau}^{ny,c} n a_{b,t-\tau}^c + \sum_{\tau=0}^{T_a} \beta_{\tau}^{ly,c} l a_{b,t-\tau}^c + \sum_{\tau=0}^{T_a} \beta_{\tau}^{dy,c} d a_{b,t-\tau}^c$$

$$+ Z_{bt} \Theta^y + \epsilon_{bt}^y.$$

$$(1)$$

The number of lags of attitude metrics is held constant at $T_y = 13$. The model also includes $T_a = 5$ lags of each advertising variable, on the theory that the direct effects of advertising on brand attitudes seem unlikely to persist beyond five weeks. The qualitative results change remarkably little with T_a , as shown in Table 20 in the appendix.

 Z_{bt} specifies the vector of fixed effects. The baseline specification includes fixed effects for each brand in the sample and for each week in the sample. Subsequent regressions also include industry/week interactions; brand/quarter interactions; and both industry/week and brand/quarter interactions.

We use the number of survey respondents for brand attitude y in week t to weight the standard errors, as brand attitudes based on larger sample sizes are more informative. Parameters for each brand attitude model y are estimated by minimizing $\{(\mathbf{N}^{\mathbf{y}}\mathbf{E}^{\mathbf{y}})'\cdot(\mathbf{N}^{\mathbf{y}}\mathbf{E}^{\mathbf{y}})\}$, where $\mathbf{N}^{\mathbf{y}} = [n_{bt}^{y}], n_{bt}^{y}$ is the number of survey respondents for brand attitude question y for brand b in week t, and $\mathbf{E}^{\mathbf{y}} = [\epsilon_{bt}^{y}]$.

5 Findings

We start by comparing fit statistics across models (Table 5). The descriptive model explains the large majority of variation in the brand attitude data, with adjusted R-squared statistics ranging from .955 to .978. These high model fit statistics are to be expected, as the brand attitude data are strongly autocorrelated, and the baseline specification includes lagged brand attitudes in addition to the 575 brand fixed effects and 252 week fixed effects.

Table 5: Model Comparison with Different Control Variables

	Model	Descriptive	Ind./Wk.	Br./Qtr.	All Controls
Adjusted	Perceived Quality	.960	.968	.964	.971
R-Squared	Perceived Value	.955	.962	.959	.966
	Recent Satisfaction	.978	.982	.980	.983
Model	Lagged Attitudes,	Yes	Yes	Yes	Yes
Includes	Advertising Variables,				
	Brand and Week Effects				
	Industry/Week Effects	No	Yes	No	Yes
	Brand/Quarter Effects	No	No	Yes	Yes

The second column of Table 5 displays the adjusted R-squared statistics when the 9,324 industry/week fixed effects are added to the descriptive model. Even though the fit statistics penalize the large increase in model complexity, the proportion of unexplained variance falls substantially, from .022-.045 in the descriptive model, to .018-.038 in the model with industry/week controls. The F-statistic rejects the null hypothesis that industry/week fixed effects should be excluded from the model (p < .001).

Similarly, the brand/quarter fixed effects reduce the proportion of unexplained variance from .022-.045 in the descriptive model to .020-.041, even after penalizing for the additional 11,500 parameters. The F-statistic rejects the null hypothesis that brand/quarter fixed effects should be excluded from the model (p < .001).

Finally, the model that includes both brand/quarter and industry/week fixed effects further reduces the proportion of unexplained variance, relative to each of the models with only a single set of control variables. The F-statistics reject the null hypotheses that industry/week fixed effects or brand/quarter fixed effects should be excluded from the model (p < .001), regardless of whether the other set of control variables is included in the baseline model or not.

The data show that, despite the limited room to improve on the descriptive model, each set of control variables is *individually and jointly* important for explaining brand attitudes. Of course, model fit statistics do not prove that the parameter estimates are unbiased or even that the results make sense. Next, we interpret and contrast the findings of the descriptive model and the all-controls model. Results from models that include industry/week controls only, and brand/quarter controls only, are provided in the appendix.

Table 6 provides all advertising parameter estimates from the descriptive and the all-controls

specifications, for each of the brand attitude models and for each type of advertising, contrasting each brand's own advertising effects with its competitors' advertising effects. Parameter estimate precision is indicated by stars for significance levels; standard errors are provided in the appendix.

The top panel of Table 6 shows that, although some of the descriptive model results are intuitive, many of them are quite challenging to interpret. For example, it is not very surprising that the first column shows that perceived quality tends to increase with one-week lags of own ad spend in both national and local media. However, the second column indicates that perceived quality also increases with competitors' ad spend in both national and local media. It certainly could be possible for a brand's attitude metrics to increase with competitors' advertising, for example, if competitors' ads draw new consumers to the category who engage in search to discover multiple brands' offerings and attributes. However, within the context of mature brands that advertise regularly, this would seem like an incongruous finding, as most of the brands in this study are already widely known at the start of the sample period. Our expectation prior to conducting this research was that brand attitudes were likely to fall, or at least not increase, with competitors' ad spend.

A greater surprise is that perceived value both increases and decreases with lagged advertising in national traditional media. The confusing pattern of both positive/significant and negative/significant results appears in all of the six media/metric/ad-type combinations with multiple statistically significant parameter estimates. In summary, such results are quite difficult to interpret and seem to cast doubt on the validity of the findings.

In contrast, the all-controls model advertising parameter estimates are more logical and more coherent, providing some reassurance that they may be closer to the true causal effects. We summarize and interpret the main findings as follows:

- Own national traditional ad spend increases all three brand attitude metrics—perceived quality, perceived value and recent satisfaction—with multiple significant lags.
- Own local traditional ad spend tends to improve perceived quality and perceived value metrics, but it does not detectably alter recent satisfaction.
- Own digital advertising increases perceived value, but does not systematically change

Table 6: Ad Parameter Estimates

Descriptive Model

Descriptive	model												
Brand Atti	tude D.V.	Perc	ceive	d Quality		Per	ceive	ed Value		Recent Satisfaction			
Ad Spend		Own		Comp.		Own		Comp.		Own	Comp.		
National	$(\tau = 0)$	4.12E-05		8.67E-05		4.00E-05	*	2.78E-04	**	2.72E-05	-9.31E-05		
Trad. Ads	$(\tau = 1)$	1.04E-04	**	2.96E-04	**	6.71E-05	**	1.10E-04		2.37E-06	-7.33E-05		
	$(\tau=2)$	-2.12E-05		-7.80E-05		5.80E-05	**	-1.51E-04		2.58E-05	-2.96E-06		
	$(\tau = 3)$	2.63E-05		-1.78E-04		4.96E-06		-9.66E-05		2.03E-05	-2.96E-04	**	
	$(\tau = 4)$	4.13E-05		1.67E-04		-1.71E-05		-1.93E-04		1.79E-05	1.54E-04	*	
	$(\tau = 5)$	-2.60E-05		-5.27E-05		-5.56E-05	**	-2.19E-04	*	-2.32E-05	-4.45E-05		
Local	$(\tau = 0)$	3.91E-05		8.32E-05		3.14E-05		-1.49E-04		-9.36E-07	4.35E-05		
Trad. Ads	$(\tau = 1)$	5.70E-05	*	-4.60E-05		2.91E-05		-1.27E-04		3.04E-05	7.80E-05		
	$(\tau=2)$	2.68E-05		2.40E-04	**	8.30E-06		2.41E-04	**	-2.54E-05	-1.47E-05		
	$(\tau = 3)$	1.29E-05		7.30E-05		-1.88E-08		-2.05E-04	*	-1.39E-05	1.92E-04	**	
	$(\tau = 4)$	1.70E-05		5.90E-05		2.60E-07		1.29E-04		-8.51E-06	3.08E-05		
	$(\tau = 5)$	-2.68E-06		-1.37E-04		4.31E-05		-4.77E-05		4.83E-06	-5.61E-05		
Digital	$(\tau = 0)$	4.29E-05		4.72E-05		8.18E-05	*	3.33E-05		1.26E-05	-4.48E-05		
Ads	$(\tau = 1)$	2.20E-05		2.08E-04		-4.19E-05		2.67E-04	*	2.21E-05	-7.25E-05		
	$(\tau=2)$	-3.48E-05		-3.26E-04	*	7.19E-05		-2.63E-04	*	1.31E-06	1.56E-04		
	$(\tau = 3)$	3.61E-05		1.23E-04		-6.42E-05		7.25E-05		4.51E-06	1.86E-04		
	$(\tau = 4)$	1.54E-06		3.19E-04	*	3.68E-05		-2.03E-04		9.13E-06	-1.16E-04		
	$(\tau = 5)$	-5.70E-05		-3.83E-04	**	4.70E-06		3.83E-04	**	4.11E-06	-1.62E-04		

All Controls Model

Brand Attit	tude D.V.	Perc	eive	d Quality		Per	ceive	ed Value		Rece	nt Sa	atisfaction	
Ad Spend		Own		Comp.		Own		Comp.		Own		Comp.	
National	$(\tau = 0)$	2.27E-05		-3.93E-04		3.26E-05		1.32E-04		2.05E-05		-9.31E-05	
Trad. Ads	$(\tau = 1)$	6.67E-05	**	-4.04E-04		7.43E-05	**	-3.70E-04		1.72E-05		7.75 E-05	
	$(\tau = 2)$	2.66E-05		-3.43E-04		6.41E-05	**	-1.84E-04		3.98E-05	*	-1.60E-05	
	$(\tau = 3)$	3.26E-05		-4.89E-04	*	1.88E-05		-3.06E-04		4.24E-05	**	-7.59E-06	
	$(\tau = 4)$	6.99E-05	**	-9.75E-05		3.22E-05		-6.98E-05		3.94E-05	*	1.01E-04	
	$(\tau = 5)$	4.81E-05	*	2.10E-05		-1.15E-05		-3.53E-04		9.08E-06		-5.57E-05	
Local	$(\tau = 0)$	2.50E-05		1.35E-04		2.91E-05		-3.25E-04		-2.00E-05		-3.31E-04	*
Trad. Ads	$(\tau = 1)$	6.54E-05	**	2.21E-04		3.60E-05		-4.28E-04	*	1.34E-05		-2.75E-04	
	$(\tau = 2)$	-8.57E-06		-5.40E-04	*	2.66E-05		4.22E-05		-2.06E-05		-7.14E-05	
	$(\tau = 3)$	3.51E-05		1.81E-04		1.03E-05		-2.41E-04		-7.85E-06		2.14E-04	
	$(\tau = 4)$	2.68E-05		-1.16E-04		7.87E-06		5.94E-05		-5.97E-06		-1.12E-04	
	$(\tau = 5)$	3.97E-05		-3.72E-04		7.78E-05	**	1.50E-04		1.49E-05		-1.15E-04	
Digital	$(\tau = 0)$	2.89E-05		1.97E-04		2.50E-05		-5.36E-04		2.94E-06		7.93E-05	
Ads	$(\tau = 1)$	6.17E-05		5.25E-04		-5.35E-05		-3.51E-04		3.04E-05		-2.02E-04	
	$(\tau = 2)$	-3.69E-05		-2.66E-04		8.18E-05	*	3.85E-04		-6.54E-07		4.28E-04	
	$(\tau = 3)$	3.40E-05		8.08E-05		-5.54E-05		2.62E-05		-2.89E-07		-3.62E-04	
	$(\tau = 4)$	-4.94E-06		-1.37E-04		2.82E-05		-1.50E-04		-8.46E-06		-2.58E-04	
	$(\tau = 5)$	6.46E-06		-7.89E-04	*	4.50E-05		7.99E-04	**	-3.37E-07		-7.72E-04	**

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

perceived quality or recent satisfaction.

- Competitors' national traditional ad spend negatively impacts perceived quality, but does not reliably change perceived value or recent satisfaction metrics.
- Competitors' local traditional advertising tends to reduce brands' perceived quality, perceived value and recent satisfaction metrics.
- Competitors' digital ads tend to reduce perceived quality and recent satisfaction measures, as expected. Perhaps surprisingly, competitor digital ads tend to increase perceived value.

Table 7 presents the estimates of lagged brand attitudes within each model. As one would expect, brand attitudes are strongly correlated across time and metrics. Inclusion of the brand/quarter control variables primarily changes the correlation between each dependent variable and its own lags from positive to negative. This is because the brand/quarter estimates control for local trends in brand attitudes, so the model including brand/quarter fixed effects produces autocorrelation parameter estimates that reflect the tendency toward local mean reversion observed in Figure 4.

To summarize the primary findings, the all-controls model indicates that (i) brand attitude metrics all rise with multiple lags of the brand's own national traditional advertising; (ii) local traditional ads increase quality and value perceptions; (iii) digital ads increase perceived value; (iv) the effects of competitors' ads are generally negative. Further, inclusion of proper control variables produces patterns of effects that appear more consistent with expectations than descriptive results without controls, without major reductions in the number of statistically significant parameter estimates.

Table 7: Parameter Estimates for Lagged Dependent Variables

Descriptive Model

Brand Attitude D.V.	Perceived Quality								Perceived V	/alue)		Recent Satisfaction					
Lagged Attitude	$q_{b,t- au}$		$v_{b,t- au}$		$s_{b,t- au}$		$q_{b,t- au}$		$v_{b,t- au}$		$s_{b,t- au}$		$q_{b,t- au}$		$v_{b,t- au}$		$s_{b,t- au}$	
$(\tau = 1)$	1.09E-01	**	2.79E-02	**	3.27E-02	**	2.55E-02	**	9.39E-02	**	4.22E-02	**	2.06E-02	**	1.87E-02	**	6.17E-02	**
$(\tau = 2)$	4.33E-02	**	1.97E-02	**	3.95E-02	**	1.90E-02	**	3.59E-02	**	4.10E-02	**	1.64E-02	**	1.86E-02	**	5.85E-02	**
$(\tau = 3)$	5.34E-02	**	1.46E-02	**	2.75E-02	**	2.40E-02	**	3.51E-02	**	2.98E-02	**	1.28E-02	**	1.45E-02	**	5.90E-02	**
$(\tau = 4)$	3.97E-02	**	2.38E-02	**	2.07E-02	**	1.16E-02	**	3.94E-02	**	1.84E-02	**	1.11E-02	**	1.26E-02	**	5.46E-02	**
$(\tau = 5)$	3.25E-02	**	1.48E-02	**	1.91E-02	**	8.37E-03	**	3.04E-02	**	2.40E-02	**	6.84E-03	**	1.24E-02	**	4.01E-02	**
$(\tau = 6)$	3.70E-02	**	1.40E-02	**	2.00E-02	**	1.29E-02	**	2.59E-02	**	2.35E-02	**	1.74E-02	**	8.71E-03	**	5.33E-02	**
$(\tau = 7)$	4.01E-02	**	9.79E-03	**	1.15E-02	**	7.73E-03	**	3.21E-02	**	1.78E-02	**	3.69E-03		9.54E-03	**	4.18E-02	**
$(\tau = 8)$	3.55E-02	**	8.45E-03	**	1.96E-02	**	1.22E-02	**	2.49E-02	**	2.03E-02	**	6.83E-03	**	1.17E-02	**	4.58E-02	**
$(\tau = 9)$	2.81E-02	**	8.52E-03	**	7.93E-03	*	5.29E-03	*	2.14E-02	**	1.50E-02	**	4.67E-03	*	2.38E-03		4.14E-02	**
$(\tau = 10)$	3.09E-02	**	9.61E-03	**	1.06E-02	**	8.15E-03	**	2.63E-02	**	1.03E-02	**	5.70E-03	**	2.28E-03		3.78E-02	**
$(\tau = 11)$	3.54E-02	**	4.70E-03		8.99E-03	*	7.98E-03	**	1.94E-02	**	6.18E-03		4.43E-03	*	7.85E-03	**	3.57E-02	**
$(\tau = 12)$	2.70E-02	**	7.91E-03	**	2.36E-02	**	5.73E-04		1.94E-02	**	6.69E-03		4.23E-03	*	1.19E-02	**	2.82E-02	**
$(\tau = 13)$	$2.25\hbox{E-}02$	**	1.87E-04		1.13E-02	**	6.68E-03	**	2.69E-02	**	8.84E-03	*	4.05E-03	*	8.76E-03	**	3.77E-02	**

All Controls Model

Brand Attitude D.V.	Perceived Quality								Perceived V	/alue			Recent Satisfaction					
Lagged Attitude	$q_{b,t- au}$		$v_{b,t- au}$		$s_{b,t- au}$		$q_{b,t- au}$		$v_{b,t- au}$		$s_{b,t- au}$		$q_{b,t- au}$		$v_{b,t- au}$		$s_{b,t- au}$	
$(\tau = 1)$	-6.21E-02	**	2.40E-02	**	2.19E-02	**	2.35E-02	**	-8.25E-02	**	3.02E-02	**	1.62E-02	**	1.34E-02	**	-1.10E-01	**
$(\tau=2)$	-1.09E-01	**	2.37E-02	**	2.78E-02	**	2.30E-02	**	-1.15E-01	**	3.10E-02	**	1.22E-02	**	1.42E-02	**	-1.14E-01	**
$(\tau = 3)$	-1.03E-01	**	2.15E-02	**	2.61E-02	**	2.44E-02	**	-1.15E-01	**	2.41E-02	**	1.37E-02	**	1.08E-02	**	-1.11E-01	**
$(\tau = 4)$	-1.09E-01	**	2.71E-02	**	2.26E-02	**	1.82E-02	**	-1.13E-01	**	2.59E-02	**	1.14E-02	**	1.28E-02	**	-1.09E-01	**
$(\tau = 5)$	-1.08E-01	**	2.27E-02	**	2.01E-02	**	1.68E-02	**	-1.10E-01	**	2.33E-02	**	1.13E-02	**	1.09E-02	**	-1.11E-01	**
$(\tau = 6)$	-9.69E-02	**	2.00E-02	**	2.20E-02	**	2.25E-02	**	-1.05E-01	**	2.28E-02	**	1.80E-02	**	5.95E-03	**	-9.93E-02	**
$(\tau = 7)$	-8.72E-02	**	1.86E-02	**	1.32E-02	**	2.10E-02	**	-9.72E-02	**	2.37E-02	**	9.67E-03	**	1.12E-02	**	-9.44E-02	**
$(\tau = 8)$	-8.73E-02	**	1.54E-02	**	2.32E-02	**	1.67E-02	**	-9.10E-02	**	2.29E-02	**	8.32E-03	**	1.43E-02	**	-8.89E-02	**
$(\tau = 9)$	-7.51E-02	**	2.00E-02	**	1.46E-02	**	1.39E-02	**	-8.50E-02	**	1.71E-02	**	8.98E-03	**	6.57E-03	**	-7.96E-02	**
$(\tau = 10)$	-6.98E-02	**	1.54E-02	**	1.38E-02	**	1.16E-02	**	-7.04E-02	**	2.05E-02	**	1.23E-02	**	9.64E-03	**	-6.56E-02	**
$(\tau = 11)$	-5.27E-02	**	1.53E-02	**	8.29E-03	*	1.55E-02	**	-6.23E-02	**	1.50E-02	**	7.31E-03	**	8.35E-03	**	-5.98E-02	**
$(\tau = 12)$	-4.63E-02	**	1.33E-02	**	1.90E-02	**	9.52E-03	**	-5.82E-02	**	1.50E-02	**	9.16E-03	**	8.77E-03	**	-5.51E-02	**
$(\tau = 13)$	-3.87E-02	**	9.21E-03	**	1.61E-02	**	8.19E-03	**	-3.90E-02	**	1.39E-02	**	6.55E-03	**	8.95E-03	**	-3.77E-02	**

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 8: Effects of Lagged Attitudes on Contemporaneous Ad Spend

Ad Spend D.V.	Nat'l Trad.	Loc. Trad.	Digital
$q_{b,t-\tau} (\tau = 1)$.006	.074	.082
(au=2)	.055	263	.154
$(\tau = 3)$.741	.091	.128
$(\tau = 4)$	268	.706 *	.028
$(\tau = 5)$	148	171	.429 *
$v_{b,t-\tau}$ $(\tau=1)$.398	.653	130
$(\tau=2)$.151	422	055
$(\tau = 3)$.329	.273	114
$(\tau = 4)$.383	.536	.087
$(\tau = 5)$	041	176	.337
$s_{b,t-\tau} (\tau = 1)$	516	.269	.134
$(\tau=2)$.059	406	.208
$(\tau = 3)$	055	.149	.420
$(\tau = 4)$.255	550	.107
$(\tau = 5)$.639	.005	222
Adj. R Squared	.770	.740	.870

^{*} Significant at the 95% confidence level.

5.1 Possible reverse causality: do lagged brand attitudes cause ad spend?

Based on our understanding of standard advertising practices, we believe that most brands do not adjust their ad spend based on recent changes in weekly brand attitudes. We believe that brands typically set quarterly or annual ad budgets, far in advance, and allocate those budgets to weeks and media vehicles in ways that typically are not driven by recent changes in brand attitude data. However, if that understanding is wrong, then some of the results reported in section 5 may be spurious.

To investigate, we reversed the all-controls specification, regressing ad spend (in each type of media) on 13 lags of each type of ad spend and five lags of each of the three brand attitude variables. Table 8 presents the parameter estimates corresponding to lags of brand attitude variables. Out of 45 parameters, only two coefficients (4%) are statistically significant at the 95% confidence level, commensurate with expected levels of Type I error. We therefore conclude that simultaneity is not a primary driver of the findings.

5.2 Ad effects by industry

Seeking a deeper understanding of the drivers of the main results, we re-estimated the all-controls model within industry-specific partitions.⁹ Table 9 presents findings from the perceived quality model with statistically significant effects in bold. Results from the perceived value and recent satisfaction models are presented in the appendix.

The main takeaway is that, despite numerous brands available for each industry, the industry-specific effects exhibit weak statistical power relative to the results calibrated on the full sample. The industry-specific estimates exhibit rates of statistical significance that approximate that expected from Type I error alone. Within national traditional ads, only 16 of 222 estimates (7.2%) are statistically significant at the 95% confidence level; comparable figures for local traditional and digital, respectively, are 12 of 222 (5.2%) and 11 of 222 (5.0%).

5.3 All Brand Attitude Metrics

We restricted primary attention in the analysis to three particular brand attitude variables that we thought were most likely to be influenced by advertising and to matter to advertisers. How do the effects look when we consider all seven available brand attitude metrics? To investigate, we estimated the all-controls model, but this time for each of the seven brand attitude metrics, and including 13 lags of all seven metrics in each of the seven models.

Table 10 ad parameter estimates for all seven models. The qualitative conclusions for the three metrics we have focused on (perceived quality, perceived value and recent satisfaction) are nearly identical to the findings reported in section 5, showing robustness of the estimates to the set of brand attitudes considered. The next three attitude metrics (willingness to recommend, general affect, proud to work) can be positively influenced by own advertising in traditional media; and the proud-to-work attitude is positively related to own digital advertising. Relationships to competitor advertising are mixed.

⁹Industry/week fixed effects were essentially replaced by a separate set of week fixed effects estimated within each partition.

Table 9: Ad Parameter Estimates by Industry on Perceived Quality

	National Traditonal Ads							I	Local Trad	litional Ad	s		Digital Ads					
	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$
Consumer Goods	4.88e-04	-3.83E-0	4 2.12E-04	5.56E-06	4.47e-04	-2.10E-04	2.60E-05	-3.77e-04	2.07E-04	-4.25E-05	-3.93e-04	1.89E-04	-9.58E-05	2.90E-04	-3.89E-04	2.23E-04	-2.80E-04	1-1.95E-04
Tools/Hardware	3.56E-04	1.05E-04	1.93E-04	-3.06E-05	-3.69E-04	2.48E-04	1.26E-04	4.32E-05	-3.22E-04	-9.24E-05	-9.45E-05	3.72E-04	1.11E-03	-1.06E-03	-7.00E-04	8.76E-04	1.12E-04	2.57E-04
Soft Drinks	-3.76E-04	1.49E-04	6.30e-04	6.74E-05	-4.52e-04	3.13E-04	2.02E-04	1.89E-04	-1.84E-04	-4.73E-04	1.94E-04	3.03E-05	8.51E-05	2.20E-04	-1.41E-04	4.07E-05	5.44E-04	-1.89E-05
Beverages: General	-1.52E-05	-4.35E-06	6-2.06E-04	-7.28E-05	5.26E-05	2.45e-04	-1.05E-04	-9.12E-05	8.75E-05	1.62E-04	1.84E-05	-5.55E-05	2.79E-04	8.87E-05	3.18E-05	-1.56E-04	2.15E-05	1.97E-04
Media Devices	1.56E-05	-1.74E-0	7-5.96E-05	1.20E-04	-9.73E-05	-1.88E-06	-6.36E-05	1.78E-04	2.60E-05	1.49E-04	2.26e-04	-1.50E-04	-2.21E-04	4.48E-04	-6.83e-04	3.63E-04	-2.35E-04	4 3.71E-04
Drugs: OTC	-2.91E-04	2.14E-04	1.52E-04	-1.09E-04	-2.20E-06	-6.79E-05	3.10E-04	-3.95e-04	-3.05E-04	2.02E-04	2.15E-04	1.82E-04	1.25E-04	1.02E-04	-2.68E-04	-5.96E-05	2.21E-05	1.64E-05
Electronics: Audio/Visual	-5.77E-05	1.94E-04	-4.54E-05	-1.77E-05	2.62e-04	-1.79E-04	-9.80E-05	-1.79E-05	-1.33E-04	1.78E-06	-3.49E-05	-1.50E-04	5.70e-04	8.58E-05	-3.64E-04	1.64E-04	2.07E-04	-4.04E-04
Internet Sites	-9.34E-05	7.77E-05	5-5.42E-06	1.73E-04	5.32E-05	3.09E-05	-1.17E-04	7.21E-06	-2.25E-04	3.28E-06	4.90E-05	-6.13E-05	1.93E-04	6.65E-04	-9.29E-05	2.55E-04	3.14E-04	2.92E-04
Home/Furnishing Stores	1.32E-04	-7.43E-05	5-7.08E-05	1.87E-04	2.64e-04	1.82E-04	-5.22E-05	1.77E-04	8.61E-05	4.82E-05	1.01E-04	1.31E-04	4.93E-05	-1.20E-05	-1.53E-04	5.89e-04	2.99E-04	-2.17E-04
Appliances	1.38E-04	-2.56E-05	5 2.68E-05	6.67E-05	-3.06E-05	-9.61E-05	1.70E-04	2.26E-04	-1.95E-06	-1.01E-04	-1.44E-04	-6.11E-05	4.33E-04	-6.08e-04	6.52e-04	7.92E-06	4.88E-05	5.14E-05
Dept. Stores	1.40E-04	-4.22E-0	72.73e-04	-2.58E-06	3.13E-05	1.93E-04	-1.51E-04	1.97E-04	-5.93E-05	1.03E-04	1.72 E-04	2.54E-04	-2.15E-05	1.08E-04	1.52E-04	2.05E-04	2.60E-05	-1.13E-04
Apparel and Shoes	2.27E-05	1.08E-04	8.15E-05	1.18E-04	1.18E-04	-2.96E-05	5.10E-05	2.54e-04	9.12E-05	8.02E-05	1.04E-05	-1.88E-05	3.62E-04	2.03E-04	-2.51E-05	1.38E-05	-1.65E-04	1 2.67E-04
Car Manufacturers	3.11E-04	2.15E-05	-1.65E-04	1.93E-04	2.06E-04	2.23E-04	-1.14E-04	-9.55E-05	-2.09E-04	-8.67E-05	1.94E-04	2.49E-05	2.44E-04	3.29E-04	9.18E-04	-4.03E-04	2.22E-04	-1.51E-04
TV Networks	3.71E-05	7.08E-05	1.61E-04	-4.54E-05	-2.16E-05	3.05e-04	-8.16E-05	2.14E-04	-1.47E-04	2.58E-04	-1.73E-04	-1.72E-04	-8.77E-05	-2.06E-05	-2.07E-04	-1.36E-06	-5.30E-05	5 2.18E-05
Hotels	-4.80E-05	-5.86E-0	5 1.32E-04	1.48E-05	1.39E-04	7.78E-05	-8.19E-05	-2.78E-05	9.55E-05	-2.14E-04	-2.30E-04	-5.03E-05	1.26E-04	4.21E-05	-2.33E-04	6.80E-05	-4.91E-05	9.93E-05
Fast Food	-7.06E-05	-1.57E-0	4-1.60E-04	1.32E-04	-1.60E-04	-1.36E-04	-5.50E-05	-6.49E-05	-4.36E-05	1.31E-04	7.96E-05	1.17E-04	-2.04E-04	-3.31E-05	-1.87E-04	-1.56E-04	-1.16E-04	4-1.34E-04
Liquor	1.27E-04	-1.39E-0	4-1.15E-04	-1.33E-04	1.44E-04	-4.24E-05	-1.74E-04	8.02E-05	6.38E-06	-7.82E-05	-6.04E-05	-6.67E-05	2.42E-04	-4.33E-05	-2.92E-04	3.64E-04	-2.77E-04	1.43E-05
Ice Cream/Pizza/Coffee	-1.06E-04	4.65e-04	1 -6.42E-05	-3.18E-04	-5.71E-07	$5.84\mathrm{E}\text{-}05$	9.64E-05	-6.59E-05	-3.22E-04	2.34E-05	1.99E-04	1.98E-04	-3.10E-04	4.92E-04	-2.22E-04	2.48E-04	-2.91E-04	1-2.77E-05
Clothing Stores	-1.27E-04	-1.40E-0	4-2.32E-04	-2.32E-05	-4.52E-06	7.12E-05	1.19E-04	-1.14E-05	2.26E-05	1.18E-04	2.91E-04	-3.60E-04	-5.40E-04	1.01E-04	3.29E-04	-2.13E-04	-3.40E-04	4 2.86E-05
Books/Kids/Office Stores	1.32E-04	4.02E-05	1.27E-04	1.07E-04	8.13E-06	2.05E-04	1.22E-04	1.04E-04	1.10E-04	5.72 E-05	2.16E-04	1.89E-04	-1.97E-04	$2.01\mathrm{E}\text{-}05$	-2.40E-04	2.50E-04	-1.31E-05	5-1.33E-04
Casual Dining	5.59E-05	1.88E-04	1.87E-04	-3.89E-05	-9.49E-05	$5.83\mathrm{E}\text{-}05$	7.06E-05	2.53E-04	-1.67E-04	-5.52E-05	-8.25E-05	1.50E-04	-3.89e-04	2.57E-04	4.86E-05	$5.87\mathrm{E}\text{-}05$	-5.72E-05	5-3.29E-04
Beer	1.03E-04	2.70E-04	2.96E-04	9.92E-05	1.96E-04	1.14E-04	2.87E-04	4.58e-04	1.46E-04	2.16E-05	2.87E-04	-3.01E-04	5.08e-04	-6.21e-04	-1.13E-04	1.61E-04	1.16E-04	-6.85E-05
Fast Casual Dining	-2.92E-06	3.96e-04	1 -6.29E-05	2.57E-04	-8.82E-05	-2.35E-04	2.66e-04	-1.83E-04	-5.90E-06	1.09E-04	-1.51E-04	4.62E-05	-2.66E-04	-1.80E-04	5.71e-04	-1.63E-04	1.68E-04	1.07E-04
Gasoline/AutoAccessories	-1.44E-04	1.70E-04	3.84E-05	-1.00E-04	1.78E-04	-2.29e-04	1.63E-04	$3.15\mathrm{E}\text{-}05$	$1.04\mathrm{E}\text{-}04$	-1.56E-04	-2.16E-05	$1.06\mathrm{E}\text{-}05$	-1.13E-04	-9.15E-05	$2.19\mathrm{E}\text{-}05$	-2.89E-04	2.28E-04	-7.34E-05
Sports/Electronics Stores	-1.98E-04	4.06E-05	5-5.57E-05	2.13E-04	-1.68E-04	1.92 E-04	-2.34E-04	-3.56E-05	3.33E-05	-2.70E-05	-1.17E-04	$2.67\mathrm{E}\text{-}05$	9.10E-05	-5.25E-05	1.38E-04	1.19E-04	-1.75E-04	1-3.08E-05
Cruise/TravelAgents	1.95E-04	1.37E-04	1.45E-04	3.16e-04	2.11E-04	-1.38E-04	1.14E-04	-4.42E-05	-1.47E-04	1.76E-04	-1.03E-04	3.23E-04	-6.20e-04	2.47E-04	3.37E-04	1.14E-04	5.38E-05	-1.54E-04
Media Services	-1.18E-04	4.59e-04	1 7.88E-05	-6.30E-05	2.03E-04	-2.26E-05	-7.42E-05	1.48E-04	-8.74E-06	1.78E-04	$8.27\mathrm{E}\text{-}05$	8.67E-06	2.23E-04	-3.48E-05	4.75E-04	-5.36E-04	3.11E-04	-3.39E-04
Insurance	-1.47E-04	8.85E-05	9.84E-05	8.75E-05	-2.14E-05	2.16E-04	-5.30E-05	-2.13E-04	3.06E-04	1.64 E-05	$5.24\mathrm{E}\text{-}05$	1.18E-04	1.54E-04	-3.41E-05	-4.26E-04	4.38E-04	-5.38E-04	13.70E-04
Steakhouses/CasualDining	7.08E-05	-1.61E-04	4 7.42E-05	-7.88E-05	1.01E-04	-6.54E-05	-3.48E-05	1.21E-04	$2.46\mathrm{E}\text{-}05$	$3.50\mathrm{E}\text{-}05$	-3.00e-04	9.79E-05	6.66E-05	-7.75E-05	-1.31E-04	1.56E-04	7.44E-05	2.43E-04
Women's Clothing Stores	2.27E-04	2.69E-04	2.61E-04	9.68E-05	1.58E-04	$2.81\mathrm{E}\text{-}04$	3.23E-05	-9.97E-05	-8.01E-05	-4.13e-04	-2.14E-04	6.92 E-05	3.52E-04	-2.45E-04	-1.05E-04	-2.41E-04	6.66e-04	6.34E-05
Airlines	9.96E-05	1.52E-04	-5.11E-05	-2.18E-05	-4.36E-05	-7.93E-05	-1.86E-05	-8.77E-05	$4.57\mathrm{E}\text{-}05$	2.21e-04	1.19E-05	2.48e-04	-4.48E-05	1.92 E-04	-1.30E-04	-3.32E-04	1.66E-04	5.67E-05
Casinos	4.90E-05	-1.22E-0	4-1.74E-04	-1.21E-04	3.70E-06	-5.01E-05	1.62E-05	-1.68E-04	-3.85E-05	1.02E-04	$1.53\mathrm{E}\text{-}04$	-2.34E-05	4.80E-05	$4.61\mathrm{E}\text{-}04$	-3.37E-04	$5.62\mathrm{E}\text{-}04$	4.22E-04	4.41E-04
Financial Services	4.82E-05	1.16E-04	-3.30E-05	1.19E-04	$2.30\mathrm{e}\text{-}04$	$1.08\mathrm{E}\text{-}04$	1.02E-04	1.95E-04	-2.25e-04	5.26E-05	$8.55\mathrm{E}\text{-}05$	-1.44E-04	2.60E-05	9.77E-06	1.72 E-04	-4.26E-04	-2.17E-04	1.33E-04
Grocery Stores	5.35E-05	-2.30E-0	43.91e-04	-2.18E-04	-1.28E-04	$7.46\mathrm{E}\text{-}05$	-4.04E-04	$5.07\mathrm{E}\text{-}05$	-3.97E-04	9.17E-05	-9.33E-05	-3.20E-05	1.43E-04	-6.58E-05	-1.42E-04	-1.58E-05	-3.95E-05	5 1.12E-04
Drugs: General	1.66E-04	-1.46E-0	4-1.32E-04	-9.10E-05	1.65E-05	1.37E-04	2.12E-05	-1.50E-05	1.35E-04	8.29E-05	-5.35E-05	-9.88E-06	-5.85E-05	-5.37E-04	3.40E-04	$7.74\mathrm{E}\text{-}05$	-4.12E-05	5 2.42E-04
Drugs: Prescription	-2.99E-05	3.06E-05	-2.45E-04	1.38E-04	-8.10E-05	1.59E-04	3.34E-04	3.07E-05	-9.73E-05	1.52 E-04	4.65 E-05	2.92E-04	2.06E-04	1.63E-04	-4.09E-04	2.02E-04	-4.24E-04	4.36E-05
Consumer Banks	-2.26E-04	-7.01E-0	5 1.10E-04	-1.45E-04	-1.82E-04	-8.28E-05	8.38E-05	-4.08E-05	-3.79E-05	9.34 E-05	-5.13E-05	-2.80E-05	-2.91E-05	2.66E-04	5.96E-05	$1.47\mathrm{E}\text{-}05$	-1.82E-04	4-1.16E-05

Note: Estimates in bold are statistically significant at the 95% level.

The final attitude metric (heard about) is extremely strongly related to all lags of own advertising in traditional media. These results are unsurprising; the survey instrument explicitly asks about recent advertising exposure. What is surprising is the absence of any detectable relationship between "heard about" and own digital advertising. However, it is the case that "heard about" decreases with contemporaneous competitor digital advertising. Recall that YouGov panelists answer brand attitude questions online, so the results came from respondents who may even be skewed more toward digital advertising exposures than the overall population.

5.4 Temporal aggregation

A frequent question in the advertising literature is how temporal (dis)aggregation affects estimation results (see, e.g., Tellis and Franses 2006 and references therein). To investigate, we aggregated the brand attitude and ad spend variables into two-week and four-week intervals, then ran comparable versions of the all-controls specification within each dataset. The qualitative results using two-week interval data, which are provided in Table 23 in the appendix, are very similar to weekly-level all-controls model. The four-week results in Table 24 are also quite similar, though less so. The aggregated data yield higher proportions of advertising parameters that are statistically significant at the 95% level, with 39% of advertising parameters exhibiting statistical significance in the four-week data, followed by 31% and 20% in the two-week and one-week datasets, respectively. We favor the results based on weekly data, as we believe that they are more conservative and that the weekly data enable better controls for unobserved confounds.

6 Conclusions, Limitations and Implications

In this research, we analyzed a unique "large-N, large-T" panel dataset of brand attitudes and advertising expenditures to investigate three specific research questions. We applied straightforward models to comparable metrics to provide a first evaluation of how ads in different media may change consumers' brand attitudes, subject to a clear identifying assumption. We further showed how those effects are impacted by various controls for unobserved variables, finding that industry/week and brand/quarter fixed effects are individually and jointly important control variables whose inclusion brings advertising parameter estimates closer to expectations without

Table 10: Ad Parameter Estimates for All Brand Attitude D.V.'s

7	T. D			******			** 1
Brand Attitude	Perceived	Perceived	Recent	Willing to	General	Proud to	Heard
D.V.	Quality	Value		Recommend		Work	About
Own $(\tau = 0)$	3.06E-05	3.89E-05	2.35E-05	7.90E-06	2.11E-05	3.37E-05	1.32E-04 **
Nat'l $(\tau = 1)$	6.39E-05 **		1.59E-05	6.40E-05 **		6.03E-05 **	
Trad. $(\tau = 2)$	1.49E-05	5.19E-05 *	3.48E-05 *	6.63E-06	8.24E-06	-5.91E-06	1.23E-04 **
Ads $(\tau = 3)$	1.93E-05	7.84E-06	3.76E-05 *	3.55E-05	1.74E-05	4.47E-05 *	9.23E-05 **
$(\tau = 4)$	5.32E-05 *	1.80E-05	3.26E-05 *	5.94E-06	-5.74E-06	1.24E-05	1.00E-04 **
$(\tau = 5)$	2.67E-05	-2.94E-05	2.44E-06	5.57E-06	2.22E-06	1.96E-05	1.12E-04 **
Own $(\tau = 0)$	2.91E-05	3.17E-05	-1.87E-05	5.21E-05 *	3.85E-05	3.48E-05	1.29E-04 **
Local $(\tau = 1)$	6.24E-05 **	3.29E-05	1.22E-05	3.68E-05	6.67E-05 **	8.39E-05 **	
Trad. $(\tau = 2)$	-1.85E-05	1.60E-05	-2.60E-05	1.97E-05	6.37E-08	3.00E-05	1.03E-04 **
Ads $(\tau = 3)$	2.64E-05	1.11E-06	-1.22E-05	-6.13E-06	4.66E-05	3.37E-05	1.10E-04 **
$(\tau = 4)$	1.41E-05	-2.59E-06	-1.02E-05	2.68E-05	5.78E-06	2.25E-05	5.95E-05 **
$(\tau = 5)$	2.33E-05	6.45E-05 **	8.77E-06	1.39E-05	3.62E-05	-2.28E-05	9.75E-05 **
$\overline{\text{Own}} (\tau = 0)$	2.54E-05	2.40E-05	1.37E-06	5.22E-05	9.35E-06	1.20E-04 **	5.80E-05
Digital $(\tau = 1)$	5.63E-05	-5.93E-05	2.62E-05	-6.81E-05	4.94E-05	-2.25E-05	-2.24E-05
Ads $(\tau = 2)$	-4.26E-05	7.85E-05	-2.94E-06	6.13E-05	2.83E-05	2.11E-05	4.68E-05
$(\tau = 3)$	2.83E-05	-6.03E-05	-3.02E-06	-1.66E-06	8.22E-07	-1.13E-05	4.38E-05
$(\tau = 4)$	-1.09E-05	2.29E-05	-1.03E-05	1.72E-05	4.28E-05	-1.19E-05	1.93E-05
$(\tau = 5)$	-1.23E-05	2.81E-05	-8.79E-06	5.10E-06	-2.87E-05	1.87E-05	4.27E-05
$\overline{\text{Comp. } (\tau = 0)}$	-4.46E-04 *	1.06E-04	-1.09E-04	1.28E-05	1.43E-04	8.59E-05	-1.80E-04
Nat'l $(\tau = 1)$	-4.36E-04 *	-3.87E-04	6.75 E-05	-5.84E-04 **	-2.58E-04	2.51E-05	-8.95E-04 **
Trad. $(\tau = 2)$	-3.42E-04	-1.70E-04	-1.42E-05	-1.51E-04	-3.30E-04	1.54E-04	-1.87E-04
Ads $(\tau = 3)$	-4.95E-04 *	-3.00E-04	-1.64E-05	2.92E-04	2.00E-05	5.17E-04 *	-6.53E-04 **
$(\tau = 4)$	-9.49E-05	-4.91E-05	9.86E-05	-2.92E-04	7.19E-05	-1.40E-04	1.60E-04
$(\tau = 5)$	4.92E-05	-3.33E-04	-4.89E-05	-2.52E-04	9.01E-05	-2.22E-04	-1.89E-04
$\overline{\text{Comp.}} (\tau = 0)$	1.37E-04	-3.25E-04	-3.23E-04 *	-3.99E-04	-1.05E-04	3.05E-04	-2.40E-05
Local $(\tau = 1)$	2.30E-04	-4.09E-04	-2.62E-04	1.73E-04	3.42E-04	-3.80E-04	5.03E-06
Trad. $(\tau = 2)$	-5.25E-04 *	4.97E-05	-6.31E-05	1.29E-05	6.63E-05	-6.73E-05	4.85E-05
Ads $(\tau = 3)$	2.04E-04	-2.17E-04	2.28E-04	-1.06E-04	4.44E-04 *	-1.55E-05	9.24E-05
$(\tau = 4)$	-8.36E-05	6.34E-05	-1.01E-04	1.10E-04	3.22E-05	-8.14E-06	-3.09E-04
$(\tau = 5)$	-3.38E-04	1.82E-04	-1.03E-04	9.54E-05	1.08E-04	2.62E-04	-1.00E-04
Comp. $(\tau = 0)$	1.59E-04	-5.74E-04	6.02E-05	6.28E-04 *	-1.06E-03 **	1.90E-04	-6.59E-04 *
Digital $(\tau = 1)$	5.16E-04	-3.56E-04	-2.19E-04	-5.35E-04	1.03E-03 **		-5.55E-04
Ads $(\tau = 2)$	-2.47E-04	4.11E-04	4.33E-04	1.01E-04	6.02E-04	-4.38E-04	-4.63E-04
$(\tau = 3)$	1.40E-04	7.19E-05	-3.33E-04	4.05E-04	-2.56E-04	-3.25E-04	1.14E-04
$(\tau = 4)$	-1.12E-04	-1.32E-04	-2.58E-04	-1.54E-04	6.82E-04 *	2.74E-04	8.20E-05
$(\tau = 5)$	-7.82E-04 *		-7.97E-04 **		-4.80E-04	1.62E-04	-2.40E-04
Adj. R Squared		.966	.983	.968	.972	.961	.947
* 0: :0	1 0504 0						

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

major reductions in estimation precision. Although the controls employed may not apply perfectly to every brand in the sample, we believe that the identifying assumption is reasonable for most of the brands considered, and that the overall results are likely to approximate the true effects.

The primary learnings indicate that (i) brand attitude metrics all rise with multiple lags of the brand's own national traditional advertising; (ii) local traditional ads increase perceived quality and perceived value; (iii) digital ads increase perceived value; and (iv) the effects of competitors' ads are generally negative. The qualitative results are robust, as the data indicate that they are not solely driven by the set of brand attitudes considered, the number of lags of ad spend included in the model, the assumption that ad spend precedes brand attitudes, or the temporal disaggregation of the data.

In particular, the data seemed to indicate that own digital advertising was less impactful on brand attitudes than national traditional and local traditional media. The rapid growth in digital advertising expenditures may reflect efforts that are focused more on direct response than branding efforts, or are more effective in harming competing brands than on building own brands. It also could be that the large brands such as P&G and GM which have raised public questions about digital advertising cost-effectiveness are correct, and that the findings of Lewis and Rao (2015) and Blake et al. (2015) about small digital ad effects on sales also apply to digital ad effects on brand attitudes. It is also entirely possible that the measures of digital ad spend contain greater measurement error than the measures of traditional ad spend, leading digital estimates to be biased downward. On the other hand, competitor digital ads influenced all three brand attitude metrics considered, so it is possible to find significant effects of digital ads on brand attitudes. The data do not allow us to disentangle these competing hypotheses, so we view these as important and compelling questions for further research.

We hope that the findings and control strategies offered may aid marketers and their agencies in using data to guide important practical questions such as whether to advertise, how much to spend, and how to allocate ad budgets. Such empirical guidance may be especially needed in industries where available data complicate the estimation of causal effects of ads on sales, such as markets with long purchase cycles or long inter-purchase times. However, it is important to note that the concerns about statistical power that have been raised in the advertising/sales literature also apply to advertising effects on brand attitudes. Practitioners interested in estimating precise effects of ad spend on brand attitudes should seriously consider running digital experiments, randomizing traditional ad spend across time and geography, and using one of the quasi-experimental approaches outlined in section 3. The data analyzed in this paper provide insufficient power to estimate precise industry-specific effects, so brand-specific effects would be even more difficult to estimate. It seems unlikely that many brands can use "media mix modeling" to estimate precise ad effects on brand attitudes using their own data alone, so practitioners should exercise appropriate caution and skepticism when considering vendors that offer such services.

This research is subject to numerous caveats and limitations. Prominent among them is that the findings and control strategies only apply to the set of brands studied, i.e. mature brands that advertise regularly. We believe they will be of limited use in evolving categories, for new brands, or for brands that advertise irregularly. Understanding the links between ad spend and brand attitudes in those situations therefore remains as another topic for future research, as it likely requires customized approaches to control for unobserved variables that drive both firm advertising and brand attitudes.

We believe the most important implication of these findings is a renewed call for highly powered field experiments. Ideally these would run simultaneously across multiple types of media, vary treatments across time and space, allow for interactions between media, and estimate treatment effects on multiple comparable behavioral and attitudinal metrics. In particular, such ambitions should become increasingly feasible as more TV advertising is delivered digitally and additional targeting capabilities are brought to market (Tuchman et al. 2017). We believe the advertising industry will eventually reach the point that scientific understanding of causal ad effects is used to set media budgets that can be provably linked to profit-relevant outcomes. We hope the results in this paper will offer a useful signpost to help guide hypotheses and statistical power calculations as the industry makes progress toward such efforts.

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Appendix

This appendix presents information and results that are not included in the main body for brevity. Table 11 lists all brands in the sample by industry. Tables 12-15 present ad parameter estimates and their standard errors in descriptive models, models with industry/week controls, models with brand/quarter controls, and all-controls models, respectively. Tables 16-19 present parameter estimates and standard errors for lagged dependent variables in all four models. Table 20 presents ad parameter estimate variation with number of lags included in the perceived quality all-controls model specification. Tables 21 and 22 report industry-specific ad parameters perceived value and recent satisfaction models. Tables 23 and 24 indicate results for the all-controls models estimated in data aggregated into two-week and four-week intervals.

Table 11: Summary of Brands in YouGov Data by Industry

Industry	All Brands
Consumer Goods	Betty Crocker, Campbell's, Charmin, Clorox, Colgate, Crest, Dawn, Gillette, M&M's, Nabisco, Pillsbury, Quaker, Schick, Snickers, Tide
Tools/Hardware	Bosch, Craftsman, DeWalt, Lincoln Electric
Soft Drinks	7UP, A & W, Coca Cola, Dr. Pepper, Mountain Dew, Pepsi, Red Bull, Sprite
Beverages: General	Crystal Light, Dasani, Folgers, Gatorade, Green Mountain, Lipton, Maxwell House, Minute Maid, Motts, Powerade, Snapple, Tropicana, V8
Media Devices	Acer, Apple, BlackBerry, Brother, Canon, Dell, Gateway, HP, IBM, Intel, LG, Motorola, Nintendo, Nokia, Samsung, Sony, Toshiba
Drugs: OTC	Advil, Aleve, Alka-Seltzer, Benadryl, Centrum, Claritin, Metamucil, Nasonex, Neosporin, One-A-Day, Preparation-H, Tums, Tylenol
Electronics: Audio/Visual	Bose, Hitachi, JVC, Kenwood, LG, Panasonic, Philips, Pioneer, RCA, Samsung, Sharp, Sony, Toshiba, Yamaha, Zenith
Internet Sites	AOL, Ask.com, cnet.com, eBay, Facebook, Google, MSN, myspace, Netflix, Yahoo!, YouTube
Home/Furnishing Stores	99 Cents Only, Ace Hardware, Bed Bath and Beyond, Crate & Barrel, Dollar General, Dollar Tree, Home Depot, Home Goods, IKEA, La-Z-Boy, Lowe's, Pier 1 Imports, Pottery Barn, True Value, Williams-Sonoma
Appliances	Bosch, Electrolux, GE, Gibson, Haier America, Kenmore, Lennox, LG, Maytag, Sub-Zero, Viking, Westinghouse, Whirlpool
Dept. Stores	Big Lots, BJ's Wholesale, Bloomingdale's, Cost Plus World Market, Costco, Dillard's, Family Dollar, J.C. Penney, Kohl's, Lord & Taylor, Macy's, Marshall's, Neiman Marcus,
Apparel and Shoes	Nordstrom, Ross, Saks, Sam's Club, Sears, Stein Mart, Target, TJ Maxx, Wal-Mart Adidas, Brooks Brothers, Calvin Klein, Coach, Converse, Eddie Bauer, Fossil, K-Swiss, Kenneth Cole,
Car Manufacturers	Levi's, Nike, Nine West, North Face, Polo Ralph Lauren, Puma, Quiksilver, Reebok, Skechers, Timberland Acura, Audi, BMW, Buick, Cadillac, Chevrolet, Chrysler, Dodge, Ford, Honda, Infiniti, Jeep,
TV Networks	Lexus, Lincoln, Mazda, Mercedes, Mercury, Nissan, Toyota, Volkswagen, Volvo ABC, Bloomberg Television, C-SPAN, CBS, CNBC, CNN, CW, ESPN, FOX, NBC, PBS, Telemundo,
	The Golf Channel, The Weather Channel, truTV, Univision
Hotels	Best Western, Comfort Inn, Courtyard by Marriott, Days Inn, Doubletree, Econo Lodge, Four Seasons, Hampton Inn, Hilton, Holiday Inn, Hyatt, La Quinta Inn, Marriott, Omni Hotels, Radisson, Ramada, Red Roof Inn, Ritz-Carlton, Sheraton, Super 8 Motels, W Hotels, Westin, Wyndham Hotels & Resorts
Fast Food	Arby's, Baja Fresh, Burger King, Carl's Jr, Chipotle, Church's, Hardee's, Jack In the Box, KFC, Krystal, Long John Silvers, McDonald's, Popeyes, Quiznos, Schlotzsky's, Subway, Taco Bell, Wendy's, Whataburger, White Castle, Wienerschnitzel
Liquor	Absolut, Bacardi, Captain Morgan, Crown Royal, Grey Goose, Hennessy, Jack Daniel's, Jim Beam, Johnnie Walker, Jose Cuervo, Maker's Mark, Smirnoff, Southern Comfort
Ice Cream/Pizza/Coffee	Baskin Robbins, Caribou Coffee, Cold Stone Creamery, Culver's, Dairy Queen, Domino's, Donatos, Dunkin' Donuts, Giordanos, Krispy Kreme, Little Caesar's, Old Chicago Pasta & Pizza, Papa John's,
Clothing Stores	Papa Murphy's, Pizza Hut, Round Table Pizza, Starbucks, Tim Horton's American Eagle, Banana Republic, Bealls, Gap, Men's Wearhouse, Old Navy, Urban Outfitters
Books/Kids/Office Stores	Athlete's Foot, Babies R Us, Barnes & Noble, Bon Ton, Famous Footwear, Jared, Kay, Office Depot, OfficeMax, Payless, Shoe Carnival, Staples, The Finish Line, Tiffany & Co., Toys R Us, Zales
Casual Dining	Applebee's, Bahama Breeze, Benihana, Buffalo Wild Wings, Carrabba's, Chili's, Famous Dave's, Fuddruckers, Golden Corral, HomeTown Buffet, Hooters, Houlihan's, Landry's Seafood House, Olive Garden, On The Border, Red Lobster, Red Robin, Ruby Tuesday's, Sizzler, TGI Friday's
Beer	Budweiser, Busch, Coors, Corona, Dos Equis, Guinness, Heineken, Keystone, Michelob, Miller, Molson, Samuel Adams, Yuengling
Fast Casual Dining	Blimpie, Bob Evans, Boston Market, Chick-Fil-A, Chuck E Cheese, Cosi, Denny's, Eat 'n Park, Friendly's Ice Cream, Frisch's Big Boy, IHOP, Marie Callender's, O'Charley's, Panda Express, Panera Bread, Sonic, Steak 'n' Shake, Taco Bueno, Waffle House
Gasoline/AutoAccessories	AAMCO, Advance Auto Parts, Arco, AutoZone, BP, Bridgestone, Chevron, Citgo, ConocoPhillips, Continental, Cooper Tires, Firestone, GMGoodwrench, Goodyear, Gulf, Jiffy Lube, Marathon, Michelin, Pep Boys, Shell, Sunoco, Valero
Sports/Electronics Stores	Best Buy, Big 5 Sporting Goods, Cabela's, Champs, CompUSA, Conn's, CVS, Dicks, F.Y.E, Fred's, GameStop, Hibbett Sports, P.C.Richard&Son, RadioShack, REI, Rite Aid, Sports Authority, Walgreen's
Cruise/TravelAgents	Busch Gardens, Carnival, Expedia, Holland America, Knott's Berry Farm, Norwegian Cruise Lines, Orbitz, Princess, Royal Caribbean, Sea World, Six Flags, Travelocity, travelzoo.com, Tripadvisor
Media Services	Adobe, Alltell/Western Wireless, AT&T, Cablevision, Comcast, DirecTV, Dish Network, Electronic Arts, Microsoft, Quicken, Sirius, Sprint, Symantec, T-Mobile, Time Warner Cable, US Cellular, Verizon, XM
Insurance	AAA, Aetna, Aflac, Allstate, Blue Cross/Blue Shield, CIGNA, Farmers Insurance Group, Geico, ING, Liberty Mutual, MetLife, Nationwide, New York Life, Northwestern Mutual, Progressive, Prudential, State Farm, The Hartford, Travelers, UnitedHealthcare
Steakhouses/CasualDining	Black Angus, Bonefish, Buca di Beppo, Chart House, Kona Grill, Lone Star Steakhouse, LongHorn Steakhouse, Maggiano's, McCormick & Schmick's, Morton's, Outback Steakhouse,
Women's Clothing Stores	Rainforest Cafe, Ruth's Chris, Smokey Bones BBQ & Grill, Texas Roadhouse, Tony Roma's Ann Taylor, Bebe, Fashion Bug, Forever 21, Juicy Couture, Lane Bryant, Victoria's Secret, White House/Black Market
Airlines	Aeromexico, Air Canada, Air France, AirTran, Alaska Air, American Airlines, British Airways, Delta, Emirates, Frontier, JetBlue, Lufthansa, Qantas, Singapore Airlines, Southwest, United, US Airways, Virgin Atlantic
Casinos	Bally's, Bellagio, Caesars Palace, Excalibur, Hard Rock Hotel, Harrah's, MGM Grand, Monte Carlo, Treasure Island, Venetian, Wynn Las Vegas
Financial Services	American Express, Capital One, Charles Schwab, Discover, E*TRADE, Edward Jones, Fidelity, Franklin Templeton, Goldman Sachs, J.P. Morgan, Janus, MasterCard, Merrill Lynch, Morgan Stanley, Oppenheimer, Putnam, T. Rowe Price, TD Ameritrade, UBS, Visa
Grocery Stores	7-Eleven, A&P, Albertsons, Casey's General Store, Cub Foods, Food Lion, Fresh&Easy, Giant, Giant Eagle, Harris Teeter, Kroger, Meijer, Pathmark, Piggly Wiggly, Publix, Safeway, Shaw's, Shop 'n Save, Whole Foods, Winn-Dixie
Drugs: General	Abilify, Aricept, AstraZeneca, Bristol-Myers Squibb, Enbrel, Ensure, Glucerna, Merck, PediaSure, Vesicare, Visine
Drugs: Prescription Consumer Banks	Advair, Cialis, Crestor, Lipitor, Nexium, Viagra, Zantac, Zoloft Bank of America, Barclay's, BB&T, Chase, Citibank, Comerica, Fifth-Third, HSBC, Huntington Bank, KeyBank, M&T Bank, PNC Bank, Regions Bank, SunTrust, Union Bank, US Bank, Wachovia, Wells Fargo, Zions Bank

Table 12: Ad Parameter Estimates in Descriptive Model

Brand Attitude	D.V.	Perceiv	ed Quality		Perce	ived Value		Recent	Satisfaction	1
Ad Spend		Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Own National	$(\tau = 0)$	4.12E-05	2.15E-05		4.00E-05	2.04E-05	*	2.72E-05	1.54E-05	
Trad. Ads	$(\tau = 1)$	1.04E-04	2.26E-05	**	6.71E-05	2.14E-05	**	2.37E-06	1.62E-05	
	$(\tau = 2)$	-2.12E-05	2.26E-05		5.80E-05	2.14E-05	**	2.58E-05	1.62E-05	
	$(\tau = 3)$	2.63E-05	2.26E-05		4.96E-06	2.14E-05		2.03E-05	1.62E-05	
	$(\tau = 4)$	4.13E-05	2.26E-05		-1.71E-05	2.14E-05		1.79E-05	1.62E-05	
	$(\tau = 5)$	-2.60E-05	2.15E-05		-5.56E-05	2.04E-05	**	-2.32E-05	1.54E-05	
Own Local	$(\tau = 0)$	3.91E-05	2.38E-05		3.14E-05	2.25E-05		-9.36E-07	1.70E-05	
Trad. Ads	$(\tau = 1)$	5.70E-05	2.45E-05	*	2.91E-05	2.32E-05		3.04E-05	1.76E-05	
	$(\tau=2)$	2.68E-05	2.41E-05		8.30E-06	2.28E-05		-2.54E-05	1.73E-05	
	$(\tau = 3)$	1.29E-05	2.41E-05		-1.88E-08	2.28E-05		-1.39E-05	1.72E-05	
	$(\tau = 4)$	1.70E-05	2.45E-05		2.60E-07	2.32E-05		-8.51E-06	1.75E-05	
	$(\tau = 5)$	-2.68E-06	2.38E-05		4.31E-05	2.25E-05		4.83E-06	1.70E-05	
Own Digital	$(\tau = 0)$	4.29E-05	3.82E-05		8.18E-05	3.62E-05	*	1.26E-05	2.74E-05	
Ads	$(\tau = 1)$	2.20E-05	4.58E-05		-4.19E-05	4.34E-05		2.21E-05	3.29E-05	
	$(\tau = 2)$	-3.48E-05	4.59E-05		7.19E-05	4.35E-05		1.31E-06	3.29E-05	
	$(\tau = 3)$	3.61E-05	4.59E-05		-6.42E-05	4.35E-05		4.51E-06	3.29E-05	
	$(\tau = 4)$	1.54E-06	4.58E-05		3.68E-05	4.34E-05		9.13E-06	3.29E-05	
	$(\tau = 5)$	-5.70E-05	3.81E-05		4.70E-06	3.61E-05		4.11E-06	2.73E-05	
Competitive	$(\tau = 0)$	8.67E-05	1.01E-04		2.78E-04	9.55E-05	**	-9.31E-05	7.23E-05	
National	$(\tau = 1)$	2.96E-04	1.08E-04	**	1.10E-04	1.02E-04		-7.33E-05	7.74E-05	
Trad. Ads	$(\tau = 2)$	-7.80E-05	1.06E-04		-1.51E-04	1.01E-04		-2.96E-06	7.61E-05	
	$(\tau = 3)$	-1.78E-04	1.06E-04		-9.66E-05	1.01E-04		-2.96E-04	7.61E-05	**
	$(\tau = 4)$	1.67E-04	1.07E-04		-1.93E-04	1.01E-04		1.54E-04	7.67E-05	*
	$(\tau = 5)$	-5.27E-05	1.00E-04		-2.19E-04	9.49E-05	*	-4.45E-05	7.18E-05	
Competitive	$(\tau = 0)$	8.32E-05	8.74E-05		-1.49E-04	8.28E-05		4.35E-05	6.27E-05	
Local	$(\tau = 1)$	-4.60E-05	8.98E-05		-1.27E-04	8.51E-05		7.80E-05	6.44E-05	
Trad. Ads	$(\tau = 2)$	2.40E-04	8.80E-05	**	2.41E-04	8.34E-05	**	-1.47E-05	6.31E-05	
	$(\tau = 3)$	7.30E-05	8.81E-05		-2.05E-04	8.35E-05	*	1.92E-04	6.32E-05	**
	$(\tau = 4)$	5.90E-05	8.97E-05		1.29E-04	8.49E-05		3.08E-05	6.43E-05	
	$(\tau = 5)$	-1.37E-04	8.76E-05		-4.77E-05	8.30E-05		-5.61E-05	6.28E-05	
Competitive	$(\tau = 0)$	4.72E-05	1.22E-04		3.33E-05	1.15E-04		-4.48E-05	8.73E-05	
Digital	$(\tau = 1)$	2.08E-04	1.40E-04		2.67E-04	1.32E-04	*	-7.25E-05	1.00E-04	
Ads	$(\tau = 2)$	-3.26E-04	1.40E-04	*	-2.63E-04	1.32E-04	*	1.56E-04	1.00E-04	
	$(\tau = 3)$	1.23E-04	1.39E-04		7.25E-05	1.32E-04		1.86E-04	9.99E-05	
	$(\tau = 4)$	3.19E-04	1.39E-04	*	-2.03E-04	1.31E-04		-1.16E-04	9.95E-05	
	$(\tau = 5)$	-3.83E-04	1.20E-04	**	3.83E-04	1.13E-04	**	-1.62E-04	8.58E-05	

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 13: Ad Parameter Estimates in Model with Industry/Week Control

Brand Attitude	D.V.	Perceiv	red Quality		Percei	ved Value		Recent S	Satisfaction	
Ad Spend		Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Own National	$(\tau = 0)$	4.00E-05	2.05E-05		2.63E-05	1.98E-05		2.77E-05	1.50E-05	
Trad. Ads	$(\tau = 1)$	6.51E-05	2.15E-05	**	6.15E-05	2.08E-05	**	9.40E-06	1.58E-05	
	$(\tau = 2)$	3.57E-06	2.15E-05		4.15E-05	2.08E-05	*	2.51E-05	1.58E-05	
	$(\tau = 3)$	1.24E-05	2.15E-05		-9.58E-06	2.08E-05		1.86E-05	1.58E-05	
	$(\tau = 4)$	4.65E-05	2.15E-05	*	9.09E-07	2.08E-05		9.86E-06	1.58E-05	
	$(\tau = 5)$	-1.29E-06	2.05E-05		-4.90E-05	1.98E-05	*	-2.53E-05	1.50E-05	
Own Local	$(\tau = 0)$	4.05E-05	2.30E-05		3.00E-05	2.22E-05		-1.98E-05	1.68E-05	
Trad. Ads	$(\tau = 1)$	6.72E-05	2.37E-05	**	3.19E-05	2.29E-05		2.37E-05	1.73E-05	
	$(\tau = 2)$	-2.10E-05	2.34E-05		2.51E-06	2.26E-05		-2.05E-05	1.71E-05	
	$(\tau = 3)$	2.58E-05	2.34E-05		-8.21E-06	2.25E-05		-3.83E-06	1.71E-05	
	$(\tau = 4)$	1.46E-06	2.37E-05		-1.69E-05	2.28E-05		-3.56E-06	1.73E-05	
	$(\tau = 5)$	8.31E-06	2.30E-05		4.77E-05	2.22E-05	*	2.09E-05	1.68E-05	
Own Digital	$(\tau = 0)$	3.58E-05	3.67E-05		4.96E-05	3.54E-05		1.06E-05	2.69E-05	
Ads	$(\tau = 1)$	4.56E-05	4.39E-05		-6.88E-05	4.24E-05		2.52E-05	3.21E-05	
	$(\tau = 2)$	-4.45E-05	4.40E-05		8.17E-05	4.24E-05		-2.27E-06	3.22E-05	
	$(\tau = 3)$	2.45E-05	4.40E-05		-6.10E-05	4.25E-05		1.32E-06	3.22E-05	
	$(\tau = 4)$	-1.80E-05	4.39E-05		3.44E-05	4.24E-05		3.25E-06	3.21E-05	
	$(\tau = 5)$	-3.94E-05	3.66E-05		1.92E-05	3.53E-05		7.89E-06	2.68E-05	
Competitive	$(\tau = 0)$	-3.89E-04	2.13E-04		1.38E-04	2.05E-04		-2.38E-04	1.56E-04	
National	$(\tau = 1)$	-3.30E-04	2.21E-04		-3.79E-04	2.13E-04		4.39E-05	1.62E-04	
Trad. Ads	$(\tau = 2)$	-2.59E-04	2.19E-04		-1.98E-04	2.12E-04		-1.18E-04	1.60E-04	
	$(\tau = 3)$	-3.62E-04	2.19E-04		-2.97E-04	2.11E-04		-1.25E-04	1.60E-04	
	$(\tau = 4)$	1.69E-04	2.18E-04		1.08E-04	2.11E-04		8.09E-05	1.60E-04	
	$(\tau = 5)$	3.20E-04	2.11E-04		-1.40E-04	2.04E-04		-1.05E-04	1.55E-04	
Competitive	$(\tau = 0)$	1.13E-04	2.16E-04		-3.07E-04	2.08E-04		-3.54E-04	1.58E-04	*
Local	$(\tau = 1)$	1.78E-04	2.22E-04		-3.23E-04	2.14E-04		-1.87E-04	1.62E-04	
Trad. Ads	$(\tau = 2)$	-4.79E-04	2.21E-04	*	1.94E-04	2.14E-04		9.24E-05	1.62E-04	
	$(\tau = 3)$	2.47E-04	2.21E-04		-2.21E-04	2.13E-04		3.23E-04	1.62E-04	*
	$(\tau = 4)$	-8.57E-05	2.20E-04		5.99E-05	2.12E-04		2.47E-05	1.61E-04	
	$(\tau = 5)$	-2.56E-04	2.14E-04		1.58E-04	2.07E-04		1.09E-04	1.57E-04	
Competitive	$(\tau = 0)$	-1.61E-04	3.05E-04		-7.32E-04	2.94E-04	*	1.31E-04	2.23E-04	
Digital	$(\tau = 1)$	4.51E-04	3.41E-04		-3.08E-04	3.29E-04		-1.37E-04	2.49E-04	
Ads	$(\tau = 2)$	-3.13E-04	3.40E-04		4.35E-04	3.28E-04		5.53E-04	2.49E-04	*
	$(\tau = 3)$	1.07E-04	3.40E-04		1.15E-04	3.29E-04		-2.78E-04	2.49E-04	
	$(\tau = 4)$	-1.14E-04	3.40E-04		-2.33E-04	3.28E-04		-1.80E-04	2.49E-04	
	$(\tau = 5)$	-5.11E-04	3.03E-04		4.92E-04	2.93E-04		-3.98E-04	2.22E-04	

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 14: Ad Parameter Estimates in Model with Brand/Quarter Control

Brand Attitude	D.V.	Perceiv	ed Quality		Percei	ved Value		Recent	Satisfaction	1
Ad Spend		Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Own National	$(\tau = 0)$	2.99E-05	2.22E-05		4.72E-05	2.11E-05	*	2.06E-05	1.59E-05	
Trad. Ads	$(\tau = 1)$	1.16E-04	2.25E-05	**	8.38E-05	2.14E-05	**	1.30E-05	1.61E-05	
	$(\tau = 2)$	1.51E-05	2.24E-05		8.23E-05	2.13E-05	**	4.04E-05	1.60E-05	*
	$(\tau = 3)$	5.39E-05	2.23E-05	*	3.73E-05	2.12E-05		4.13E-05	1.60E-05	**
	$(\tau = 4)$	7.88E-05	2.24E-05	**	2.31E-05	2.13E-05		4.23E-05	1.61E-05	**
	$(\tau = 5)$	4.08E-05	2.21E-05		-1.25E-05	2.10E-05		1.22E-05	1.58E-05	
Own Local	$(\tau = 0)$	1.37E-05	2.44E-05		3.36E-05	2.32E-05		-4.27E-06	1.75E-05	-
Trad. Ads	$(\tau = 1)$	4.68E-05	2.46E-05		3.73E-05	2.34E-05		2.37E-05	1.76E-05	
	$(\tau = 2)$	3.26E-05	2.44E-05		3.81E-05	2.32E-05		-2.27E-05	1.75E-05	
	$(\tau = 3)$	2.00E-05	2.43E-05		2.30E-05	2.31E-05		-1.80E-05	1.74E-05	
	$(\tau = 4)$	3.43E-05	2.44E-05		2.92E-05	2.32E-05		-8.84E-06	1.75E-05	
	$(\tau = 5)$	2.75E-05	2.43E-05		7.63E-05	2.31E-05	**	1.07E-06	1.74E-05	
Own Digital	$(\tau = 0)$	2.35E-05	3.96E-05		4.69E-05	3.77E-05		1.45E-05	2.84E-05	
Ads	$(\tau = 1)$	3.32E-05	4.42E-05		-2.82E-05	4.20E-05		2.76E-05	3.17E-05	
	$(\tau = 2)$	-3.10E-05	4.41E-05		7.39E-05	4.19E-05		3.89E-06	3.16E-05	
	$(\tau = 3)$	4.40E-05	4.41E-05		-4.73E-05	4.19E-05		7.00E-06	3.16E-05	
	$(\tau = 4)$	2.06E-05	4.42E-05		4.15E-05	4.20E-05		9.16E-06	3.17E-05	
	$(\tau = 5)$	-1.07E-05	3.93E-05		3.79E-05	3.74E-05		1.47E-05	2.82E-05	
Competitive	$(\tau = 0)$	-5.64E-05	1.02E-04		3.84E-04	9.68E-05	**	-5.68E-05	7.30E-05	
National	$(\tau = 1)$	2.72E-04	1.06E-04	*	2.37E-04	1.00E-04	*	-2.27E-05	7.57E-05	
Trad. Ads	$(\tau = 2)$	-1.81E-05	1.05E-04		8.88E-05	9.99E-05		7.15E-05	7.53E-05	
	$(\tau = 3)$	-1.42E-04	1.04E-04		8.89E-05	9.92E-05		-2.45E-04	7.48E-05	**
	$(\tau = 4)$	1.85E-04	1.05E-04		-5.47E-05	9.94E-05		1.18E-04	7.50E-05	
	$(\tau = 5)$	2.30E-05	1.03E-04		-1.57E-05	9.82E-05		-3.27E-05	7.41E-05	
Competitive	$(\tau = 0)$	7.29E-05	8.94E-05		-1.21E-04	8.50E-05		1.17E-05	6.41E-05	
Local	$(\tau = 1)$	-3.12E-05	8.98E-05		-1.41E-04	8.53E-05		6.36E-05	6.43E-05	
Trad. Ads	$(\tau = 2)$	2.39E-04	8.90E-05	**	1.66E-04	8.46E-05	*	-3.69E-05	6.38E-05	
	$(\tau = 3)$	1.11E-04	8.88E-05		-2.33E-04	8.44E-05	**	1.67E-04	6.36E-05	**
	$(\tau = 4)$	9.09E-05	8.96E-05		7.05E-05	8.52E-05		4.11E-05	6.42E-05	
	$(\tau = 5)$	-9.71E-05	9.02E-05		-9.44E-05	8.57E-05		-3.23E-05	6.46E-05	
Competitive	$(\tau = 0)$	-7.18E-05	1.26E-04		-3.43E-05	1.20E-04		2.16E-05	9.05E-05	
Digital	$(\tau = 1)$	1.41E-04	1.36E-04		1.89E-04	1.29E-04		-5.22E-05	9.76E-05	
Ads	$(\tau = 2)$	-4.00E-04	1.35E-04	**	-2.83E-04	1.28E-04	*	1.54E-04	9.68E-05	
	$(\tau = 3)$	4.82E-05	1.35E-04		-3.16E-05	1.28E-04		1.54E-04	9.67E-05	
	$(\tau = 4)$	3.28E-04	1.34E-04	*	-2.65E-04	1.28E-04	*	-3.63E-05	9.63E-05	
	$(\tau = 5)$	-3.45E-04	1.24E-04	**	3.71E-04	1.18E-04	**	-6.65E-05	8.91E-05	

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 15: Ad Parameter Estimates in All Controls Model

Brand Attitude	e D.V.	Perceiv	ed Quality		Percei	ived Value		Recent	Satisfaction	1
Ad Spend		Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Own National	$(\tau = 0)$	2.27E-05	2.12E-05		3.26E-05	2.05E-05		2.05E-05	1.55E-05	
Trad. Ads	$(\tau = 1)$	6.67E-05	2.15E-05	**	7.43E-05	2.08E-05	**	1.72E-05	1.57E-05	
	$(\tau = 2)$	2.66E-05	2.14E-05		6.41E-05	2.07E-05	**	3.98E-05	1.57E-05	*
	$(\tau = 3)$	3.26E-05	2.14E-05		1.88E-05	2.07E-05		4.24E-05	1.56E-05	**
	$(\tau = 4)$	6.99E-05	2.15E-05	**	3.22E-05	2.08E-05		3.94E-05	1.57E-05	*
	$(\tau = 5)$	4.81E-05	2.11E-05	*	-1.15E-05	2.04E-05		9.08E-06	1.55E-05	
Own Local	$(\tau = 0)$	2.50E-05	2.37E-05		2.91E-05	2.29E-05		-2.00E-05	1.74E-05	
Trad. Ads	$(\tau = 1)$	6.54E-05	2.39E-05	**	3.60E-05	2.31E-05		1.34E-05	1.75E-05	
	$(\tau=2)$	-8.57E-06	2.37E-05		2.66E-05	2.30E-05		-2.06E-05	1.74E-05	
	$(\tau = 3)$	3.51E-05	2.37E-05		1.03E-05	2.29E-05		-7.85E-06	1.73E-05	
	$(\tau = 4)$	2.68E-05	2.37E-05		7.87E-06	2.30E-05		-5.97E-06	1.74E-05	
	$(\tau = 5)$	3.97E-05	2.36E-05		7.78E-05	2.29E-05	**	1.49E-05	1.73E-05	
Own Digital	$(\tau = 0)$	2.89E-05	3.83E-05		2.50E-05	3.70E-05		2.94E-06	2.80E-05	
Ads	$(\tau = 1)$	6.17E-05	4.25E-05		-5.35E-05	4.11E-05		3.04E-05	3.11E-05	
	$(\tau = 2)$	-3.69E-05	4.24E-05		8.18E-05	4.10E-05	*	-6.54E-07	3.10E-05	
	$(\tau = 3)$	3.40E-05	4.24E-05		-5.54E-05	4.11E-05		-2.89E-07	3.11E-05	
	$(\tau = 4)$	-4.94E-06	4.25E-05		2.82E-05	4.11E-05		-8.46E-06	3.11E-05	
	$(\tau = 5)$	6.46E-06	3.79E-05		4.50E-05	3.67E-05		-3.37E-07	2.77E-05	
Competitive	$(\tau = 0)$	-3.93E-04	2.20E-04		1.32E-04	2.13E-04		-9.31E-05	1.61E-04	
National	$(\tau = 1)$	-4.04E-04	2.22E-04		-3.70E-04	2.14E-04		7.75E-05	1.62E-04	
Trad. Ads	$(\tau = 2)$	-3.43E-04	2.19E-04		-1.84E-04	2.12E-04		-1.60E-05	1.61E-04	
	$(\tau = 3)$	-4.89E-04	2.18E-04	*	-3.06E-04	2.11E-04		-7.59E-06	1.60E-04	
	$(\tau = 4)$	-9.75E-05	2.18E-04		-6.98E-05	2.11E-04		1.01E-04	1.59E-04	
	$(\tau = 5)$	2.10E-05	2.18E-04		-3.53E-04	2.11E-04		-5.57E-05	1.60E-04	
Competitive	$(\tau = 0)$	1.35E-04	2.20E-04		-3.25E-04	2.13E-04		-3.31E-04	1.61E-04	*
Local	$(\tau = 1)$	2.21E-04	2.22E-04		-4.28E-04	2.15E-04	*	-2.75E-04	1.62E-04	
Trad. Ads	$(\tau = 2)$	-5.40E-04	2.23E-04	*	4.22E-05	2.16E-04		-7.14E-05	1.63E-04	
	$(\tau = 3)$	1.81E-04	2.22E-04		-2.41E-04	2.15E-04		2.14E-04	1.63E-04	
	$(\tau = 4)$	-1.16E-04	2.21E-04		5.94E-05	2.14E-04		-1.12E-04	1.62E-04	
	$(\tau = 5)$	-3.72E-04	2.22E-04		1.50E-04	2.15E-04		-1.15E-04	1.62E-04	
Competitive	$(\tau = 0)$	1.97E-04	3.16E-04		-5.36E-04	3.05E-04		7.93E-05	2.31E-04	
Digital	$(\tau = 1)$	5.25E-04	3.33E-04		-3.51E-04	3.22E-04		-2.02E-04	2.44E-04	
Ads	$(\tau=2)$	-2.66E-04	3.32E-04		3.85E-04	3.21E-04		4.28E-04	2.43E-04	
	$(\tau = 3)$	8.08E-05	3.32E-04		2.62E-05	3.22E-04		-3.62E-04	2.43E-04	
	$(\tau = 4)$	-1.37E-04	3.32E-04		-1.50E-04	3.21E-04		-2.58E-04	2.43E-04	
	$(\tau = 5)$	-7.89E-04	3.13E-04	*	7.99E-04	3.03E-04	**	-7.72E-04	2.29E-04	**

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 16: Parameter Estimates for Lagged D.V.'s in Descriptive Model

Brand Attitu	ide D.V.	Perceiv	ved Quality	,	Perce	ived Value		Recent	Satisfaction	n
Lagged Attit	ude	Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Log Quality	$(\tau = 1)$	1.09E-01	2.66E-03	**	2.55E-02	2.52E-03	**	2.06E-02	1.91E-03	**
	$(\tau = 2)$	4.33E-02	2.68E-03	**	1.90E-02	2.54E-03	**	1.64E-02	1.92E-03	**
	$(\tau = 3)$	5.34E-02	2.68E-03	**	2.40E-02	2.54E-03	**	1.28E-02	1.92E-03	**
	$(\tau = 4)$	3.97E-02	2.69E-03	**	1.16E-02	2.54E-03	**	1.11E-02	1.92E-03	**
	$(\tau = 5)$	3.25E-02	2.69E-03	**	8.37E-03	2.55E-03	**	6.84E-03	1.93E-03	**
	$(\tau = 6)$	3.70E-02	2.69E-03	**	1.29E-02	2.55E-03	**	1.74E-02	1.93E-03	**
	$(\tau = 7)$	4.01E-02	2.69E-03	**	7.73E-03	2.55E-03	**	3.69E-03	1.93E-03	
	$(\tau = 8)$	3.55E-02	2.69E-03	**	1.22E-02	2.54E-03	**	6.83E-03	1.93E-03	**
	$(\tau = 9)$	2.81E-02	2.69E-03	**	5.29E-03	2.55E-03	*	4.67E-03	1.93E-03	*
	$(\tau = 10)$	3.09E-02	2.69E-03	**	8.15E-03	2.55E-03	**	5.70E-03	1.93E-03	**
	$(\tau = 11)$	3.54E-02	2.69E-03	**	7.98E-03	2.54E-03	**	4.43E-03	1.93E-03	*
	$(\tau = 12)$	2.70E-02	2.68E-03	**	5.73E-04	2.54E-03		4.23E-03	1.92E-03	*
	$(\tau = 13)$	2.25E-02	2.66E-03	**	6.68E-03	2.52E-03	**	4.05E-03	1.91E-03	*
Log Value	$(\tau = 1)$	2.79E-02	2.81E-03	**	9.39E-02	2.66E-03	**	1.87E-02	2.01E-03	**
	$(\tau=2)$	1.97E-02	2.82E-03	**	3.59E-02	2.67E-03	**	1.86E-02	2.02E-03	**
	$(\tau = 3)$	1.46E-02	2.83E-03	**	3.51E-02	2.68E-03	**	1.45E-02	2.03E-03	**
	$(\tau = 4)$	2.38E-02	2.83E-03	**	3.94E-02	2.68E-03	**	1.26E-02	2.03E-03	**
	$(\tau = 5)$	1.48E-02	2.83E-03	**	3.04E-02	2.68E-03	**	1.24E-02	2.03E-03	**
	$(\tau = 6)$	1.40E-02	2.84E-03	**	2.59E-02	2.69E-03	**	8.71E-03	2.03E-03	**
	$(\tau = 7)$	9.79E-03	2.84E-03	**	3.21E-02	2.69E-03	**	9.54E-03	2.03E-03	**
	$(\tau = 8)$	8.45E-03	2.84E-03	**	2.49E-02	2.69E-03	**	1.17E-02	2.03E-03	**
	$(\tau = 9)$	8.52E-03	2.84E-03	**	2.14E-02	2.69E-03	**	2.38E-03	2.03E-03	
	$(\tau = 10)$	9.61E-03	2.84E-03	**	2.63E-02	2.69E-03	**	2.28E-03	2.03E-03	
	$(\tau = 11)$	4.70E-03	2.83E-03		1.94E-02	2.68E-03	**	7.85E-03	2.03E-03	**
	$(\tau = 12)$	7.91E-03	2.83E-03	**	1.94E-02	2.68E-03	**	1.19E-02	2.03E-03	**
	$(\tau = 13)$	1.87E-04	2.82E-03		2.69E-02	2.67E-03	**	8.76E-03	2.02E-03	**
Log Recent	$(\tau = 1)$	3.27E-02	3.70E-03	**	4.22E-02	3.51E-03	**	6.17E-02	2.66E-03	**
Satisfaction	$(\tau=2)$	3.95E-02	3.71E-03	**	4.10E-02	3.52E-03	**	5.85E-02	2.66E-03	**
	$(\tau = 3)$	2.75E-02	3.72E-03	**	2.98E-02	3.53E-03	**	5.90E-02	2.67E-03	**
	$(\tau = 4)$	2.07E-02	3.73E-03	**	1.84E-02	3.53E-03	**	5.46E-02	2.67E-03	**
	$(\tau = 5)$	1.91E-02	3.74E-03	**	2.40E-02	3.54E-03	**	4.01E-02	2.68E-03	**
	$(\tau = 6)$	2.00E-02	3.74E-03	**	2.35E-02	3.54E-03	**	5.33E-02	2.68E-03	**
	$(\tau = 7)$	1.15E-02	3.74E-03	**	1.78E-02	3.54E-03	**	4.18E-02	2.68E-03	**
	$(\tau = 8)$	1.96E-02	3.74E-03	**	2.03E-02	3.54E-03	**	4.58E-02	2.68E-03	**
	$(\tau = 9)$	7.93E-03	3.74E-03	*	1.50E-02	3.54E-03	**	4.14E-02	2.68E-03	**
	$(\tau = 10)$	1.06E-02	3.74E-03	**	1.03E-02	3.54E-03	**	3.78E-02	2.68E-03	**
	$(\tau = 11)$	8.99E-03	3.74E-03	*	6.18E-03	3.54E-03		3.57E-02	2.68E-03	**
	$(\tau = 12)$	2.36E-02	3.73E-03	**	6.69E-03	3.53E-03		2.82E-02	2.67E-03	**
	$(\tau = 13)$	1.13E-02	3.72 E-03	**	8.84E-03	3.53E-03	*	3.77E-02	2.67E-03	**

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 17: Parameter Estimates for Lagged D.V.'s in Model with Industry/Week Control

Brand Attitu	ide D.V.	Percei	ved Quality	7	Perce	ived Value		Recent	Satisfaction	n
Lagged Attit	ude	Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Log Quality	$(\tau = 1)$	1.09E-01	2.75E-03	**	2.87E-02	2.65E-03	**	2.13E-02	2.01E-03	**
	$(\tau = 2)$	4.76E-02	2.76E-03	**	2.32E-02	2.67E-03	**	1.46E-02	2.02E-03	**
	$(\tau = 3)$	4.98E-02	2.77E-03	**	2.21E-02	2.67E-03	**	1.47E-02	2.03E-03	**
	$(\tau = 4)$	3.81E-02	2.77E-03	**	1.30E-02	2.67E-03	**	1.03E-02	2.03E-03	**
	$(\tau = 5)$	3.30E-02	2.77E-03	**	9.01E-03	2.68E-03	**	9.76E-03	2.03E-03	**
	$(\tau = 6)$	3.79E-02	2.77E-03	**	1.47E-02	2.68E-03	**	1.57E-02	2.03E-03	**
	$(\tau = 7)$	4.04E-02	2.77E-03	**	1.21E-02	2.68E-03	**	6.27E-03	2.03E-03	**
	$(\tau = 8)$	3.13E-02	2.77E-03	**	7.37E-03	2.68E-03	**	4.29E-03	2.03E-03	*
	$(\tau = 9)$	3.39E-02	2.77E-03	**	4.98E-03	2.68E-03		5.07E-03	2.03E-03	*
	$(\tau = 10)$	2.83E-02	2.77E-03	**	4.38E-03	2.68E-03		8.32E-03	2.03E-03	**
	$(\tau = 11)$	3.61E-02	2.77E-03	**	9.25E-03	2.67E-03	**	3.19E-03	2.03E-03	
	$(\tau = 12)$	2.97E-02	2.77E-03	**	2.99E-03	2.67E-03		5.79E-03	2.03E-03	**
	$(\tau = 13)$	2.97E-02	2.75E-03	**	2.90E-03	2.65E-03		3.73E-03	2.01E-03	
Log Value	$(\tau = 1)$	2.82E-02	2.85E-03	**	8.65E-02	2.75E-03	**	1.97E-02	2.08E-03	**
_	$(\tau = 2)$	2.41E-02	2.86E-03	**	4.35E-02	2.76E-03	**	1.93E-02	2.09E-03	**
	$(\tau = 3)$	1.85E-02	2.86E-03	**	4.00E-02	2.76E-03	**	1.38E-02	2.10E-03	**
	$(\tau = 4)$	2.14E-02	2.87E-03	**	3.62E-02	2.77E-03	**	1.43E-02	2.10E-03	**
	$(\tau = 5)$	1.32E-02	2.87E-03	**	3.24E-02	2.77E-03	**	1.12E-02	2.10E-03	**
	$(\tau = 6)$	9.48E-03	2.87E-03	**	3.06E-02	2.77E-03	**	5.81E-03	2.10E-03	**
	$(\tau = 7)$	9.08E-03	2.87E-03	**	3.01E-02	2.77E-03	**	1.09E-02	2.10E-03	**
	$(\tau = 8)$	6.10E-03	2.87E-03	*	2.76E-02	2.77E-03	**	1.32E-02	2.10E-03	**
	$(\tau = 9)$	1.09E-02	2.87E-03	**	2.25E-02	2.77E-03	**	3.92E-03	2.10E-03	
	$(\tau = 10)$	6.37E-03	2.87E-03	*	2.71E-02	2.77E-03	**	7.07E-03	2.10E-03	**
	$(\tau = 11)$	8.74E-03	2.87E-03	**	2.38E-02	2.77E-03	**	6.62E-03	2.10E-03	**
	$(\tau = 12)$	7.12E-03	2.86E-03	*	1.74E-02	2.76E-03	**	7.22E-03	2.10E-03	**
	$(\tau = 13)$	4.11E-03	2.85E-03		2.73E-02	2.75E-03	**	7.79E-03	2.09E-03	**
Log Recent	$(\tau = 1)$	3.16E-02	3.74E-03	**	4.10E-02	3.62E-03	**	6.40E-02	2.74E-03	**
Satisfaction	$(\tau = 2)$	3.50E-02	3.76E-03	**	3.90E-02	3.63E-03	**	5.61E-02	2.75E-03	**
	$(\tau = 3)$	2.89E-02	3.76E-03	**	2.71E-02	3.63E-03	**	5.58E-02	2.76E-03	**
	$(\tau = 4)$	2.13E-02	3.77E-03	**	2.60E-02	3.64E-03	**	5.20E-02	2.76E-03	**
	$(\tau = 5)$	1.80E-02	3.78E-03	**	2.13E-02	3.65E-03	**	4.29E-02	2.76E-03	**
	$(\tau = 6)$	2.00E-02	3.77E-03	**	2.06E-02	3.64E-03	**	4.85E-02	2.76E-03	**
	$(\tau = 7)$	8.94E-03	3.78E-03	*	1.86E-02	3.65E-03	**	4.49E-02	2.77E-03	**
	$(\tau = 8)$	1.96E-02	3.78E-03	**	1.60E-02	3.65E-03	**	4.20E-02	2.77E-03	**
	$(\tau = 9)$	1.13E-02	3.78E-03	**	1.05E-02	3.65E-03	**	4.06E-02	2.77E-03	**
	$(\tau = 10)$	1.07E-02	3.78E-03	**	1.45E-02	3.65E-03	**	4.38E-02	2.77E-03	**
	$(\tau = 11)$	6.79E-03	3.77E-03		9.46E-03	3.64E-03	**	3.80E-02	2.76E-03	**
	$(\tau = 12)$	1.72E-02	3.77E-03	**	9.56E-03	3.64E-03	**	3.02E-02	2.76E-03	**
	$(\tau = 13)$	1.37E-02	3.76E-03	**	9.68E-03	3.63E-03	**	3.69E-02	2.75E-03	**

^{*} Significant at the 95% confidence level. ** Significant at the 99% confidence level.

Table 18: Parameter Estimates for Lagged D.V.'s in Model with Brand/Quarter Control

Brand Attitu	de D.V.	Perceiv	ed Quality		Percei	ved Value		Recent	Satisfaction	<u> </u>
Lagged Attitu	ude	Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Log Quality	$(\tau = 1)$	-6.35E-02	2.76E-03	**	2.16E-02	2.63E-03	**	1.47E-02	1.98E-03	**
3 3 3	$(\tau = 2)$	-1.16E-01	2.77E-03	**	1.88E-02	2.63E-03	**	1.29E-02	1.98E-03	**
	$(\tau = 3)$	-1.01E-01	2.78E-03	**	2.66E-02	2.64E-03	**	1.11E-02	1.99E-03	**
	$(\tau = 4)$	-1.08E-01	2.79E-03	**	1.70E-02	2.65E-03	**	1.12E-02	2.00E-03	**
	$(\tau = 5)$	-1.09E-01	2.80E-03	**	1.58E-02	2.66E-03	**	7.85E-03	2.01E-03	**
	$(\tau = 6)$	-9.82E-02	2.80E-03	**	2.02E-02	2.67E-03	**	1.84E-02	2.01E-03	**
	$(\tau = 7)$	-8.80E-02	2.81E-03	**	1.64E-02	2.67E-03	**	6.14E-03	2.01E-03	**
	$(\tau = 8)$	-8.36E-02	2.81E-03	**	2.09E-02	2.67E-03	**	9.35E-03	2.01E-03	**
	$(\tau = 9)$	-8.02E-02	2.80E-03	**	1.38E-02	2.66E-03	**	7.54E-03	2.01E-03	**
	$(\tau = 10)$	-6.75E-02	2.80E-03	**	1.46E-02	2.66E-03	**	9.56E-03	2.00E-03	**
	$(\tau = 11)$	-5.32E-02	2.79E-03	**	1.41E-02	2.65E-03	**	8.23E-03	2.00E-03	**
	$(\tau = 12)$	-4.92E-02	2.78E-03	**	6.74E-03	2.64E-03	*	7.37E-03	1.99E-03	**
	$(\tau = 13)$	-4.67E-02	2.78E-03	**	1.02E-02	2.64E-03	**	6.65E-03	1.99E-03	**
Log Value	$(\tau = 1)$	2.66E-02	2.91E-03	**	-7.45E-02	2.77E-03	**	1.36E-02	2.09E-03	**
	$(\tau = 2)$	2.22E-02	2.92E-03	**	-1.22E-01	2.78E-03	**	1.42E-02	2.09E-03	**
	$(\tau = 3)$	1.99E-02	2.94E-03	**	-1.19E-01	2.79E-03	**	1.14E-02	2.11E-03	**
	$(\tau = 4)$	3.02E-02	2.95E-03	**	-1.09E-01	2.80E-03	**	1.13E-02	2.11E-03	**
	$(\tau = 5)$	2.60E-02	2.96E-03	**	-1.12E-01	2.81E-03	**	1.30E-02	2.12E-03	**
	$(\tau = 6)$	2.55E-02	2.97E-03	**	-1.10E-01	2.82E-03	**	8.91E-03	2.12E-03	**
	$(\tau = 7)$	2.15E-02	2.97E-03	**	-9.61E-02	2.82E-03	**	1.02E-02	2.13E-03	**
	$(\tau = 8)$	2.05E-02	2.96E-03	**	-9.32E-02	2.82E-03	**	1.24E-02	2.12E-03	**
	$(\tau = 9)$	2.04E-02	2.96E-03	**	-8.72E-02	2.81E-03	**	4.10E-03	2.12E-03	
	$(\tau = 10)$	2.03E-02	2.95E-03	**	-7.34E-02	2.81E-03	**	3.91E-03	2.12E-03	
	$(\tau = 11)$	1.31E-02	2.94E-03	**	-6.82E-02	2.79E-03	**	8.05E-03	2.11E-03	**
	$(\tau = 12)$	1.50E-02	2.92E-03	**	-5.78E-02	2.78E-03	**	1.22E-02	2.09E-03	**
	$(\tau = 13)$	7.18E-03	2.91E-03	*	-4.17E-02	2.77E-03	**	9.89E-03	2.09E-03	**
Log Recent	$(\tau = 1)$	2.20E-02	3.86E-03	**	3.21E-02	3.67E-03	**	-1.14E-01	2.77E-03	**
Satisfaction	$(\tau = 2)$	3.16E-02	3.88E-03	**	3.33E-02	3.69E-03	**	-1.13E-01	2.78E-03	**
	$(\tau = 3)$	2.24E-02	3.91E-03	**	2.62E-02	3.72E-03	**	-1.07E-01	2.80E-03	**
	$(\tau = 4)$	1.83E-02	3.93E-03	**	1.81E-02	3.74E-03	**	-1.05E-01	2.82E-03	**
	$(\tau = 5)$	1.62E-02	3.95E-03	**	2.38E-02	3.75E-03	**	-1.13E-01	2.83E-03	**
	$(\tau = 6)$	1.70E-02	3.96E-03	**	2.32E-02	3.76E-03	**	-9.51E-02	2.84E-03	**
	$(\tau = 7)$	9.78E-03	3.96E-03	*	2.06E-02	3.77E-03	**	-9.78E-02	2.84E-03	**
	$(\tau = 8)$	1.66E-02	3.97E-03	**	2.56E-02	3.77E-03	**	-8.64E-02	2.84E-03	**
	$(\tau = 9)$	5.85E-03	3.96E-03		1.97E-02	3.76E-03	**	-7.89E-02	2.84E-03	**
	$(\tau = 10)$	8.36E-03	3.94E-03	*	1.48E-02	3.75E-03	**	-7.12E-02	2.83E-03	**
	$(\tau = 11)$	4.99E-03	3.93E-03		9.42E-03	3.74E-03	*	-6.33E-02	2.82E-03	**
	$(\tau = 12)$	2.14E-02	3.91E-03	**	1.01E-02	3.71E-03	**	-5.89E-02	2.80E-03	**
	$(\tau = 13)$	9.97E-03	3.89E-03	*	9.94E-03	3.70E-03	**	-3.97E-02	2.79E-03	**
* Significant		confidence								
** Significant										
9										

Table 19: Parameter Estimates for Lagged D.V.'s in All Controls Model

Brand Attitu	ide D.V.	Perceiv	red Quality		Percei	ved Value		Recent	Satisfaction	1
Lagged Attit	ude	Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Log Quality	$(\tau = 1)$	-6.21E-02	2.86E-03	**	2.35E-02	2.77E-03	**	1.62E-02	2.09E-03	**
	$(\tau = 2)$	-1.09E-01	2.87E-03	**	2.30E-02	2.77E-03	**	1.22E-02	2.10E-03	**
	$(\tau = 3)$	-1.03E-01	2.88E-03	**	2.44E-02	2.79E-03	**	1.37E-02	2.11E-03	**
	$(\tau = 4)$	-1.09E-01	2.89E-03	**	1.82E-02	2.80E-03	**	1.14E-02	2.11E-03	**
	$(\tau = 5)$	-1.08E-01	2.90E-03	**	1.68E-02	2.81E-03	**	1.13E-02	2.12E-03	**
	$(\tau = 6)$	-9.69E-02	2.91E-03	**	2.25E-02	2.82E-03	**	1.80E-02	2.13E-03	**
	$(\tau = 7)$	-8.72E-02	2.92E-03	**	2.10E-02	2.82E-03	**	9.67E-03	2.13E-03	**
	$(\tau = 8)$	-8.73E-02	2.91E-03	**	1.67E-02	2.82E-03	**	8.32E-03	2.13E-03	**
	$(\tau = 9)$	-7.51E-02	2.91E-03	**	1.39E-02	2.82E-03	**	8.98E-03	2.13E-03	**
	$(\tau = 10)$	-6.98E-02	2.90E-03	**	1.16E-02	2.81E-03	**	1.23E-02	2.12E-03	**
	$(\tau = 11)$	-5.27E-02	2.89E-03	**	1.55E-02	2.80E-03	**	7.31E-03	2.12E-03	**
	$(\tau = 12)$	-4.63E-02	2.88E-03	**	9.52E-03	2.79E-03	**	9.16E-03	2.11E-03	**
	$(\tau = 13)$	-3.87E-02	2.87E-03	**	8.19E-03	2.78E-03	**	6.55E-03	2.10E-03	**
Log Value	$(\tau = 1)$	2.40E-02	2.97E-03	**	-8.25E-02	2.87E-03	**	1.34E-02	2.17E-03	**
	$(\tau = 2)$	2.37E-02	2.97E-03	**	-1.15E-01	2.88E-03	**	1.42E-02	2.17E-03	**
	$(\tau = 3)$	2.15E-02	2.99E-03	**	-1.15E-01	2.89E-03	**	1.08E-02	2.19E-03	**
	$(\tau = 4)$	2.71E-02	3.00E-03	**	-1.13E-01	2.90E-03	**	1.28E-02	2.19E-03	**
	$(\tau = 5)$	2.27E-02	3.01E-03	**	-1.10E-01	2.91E-03	**	1.09E-02	2.20E-03	**
	$(\tau = 6)$	2.00E-02	3.01E-03	**	-1.05E-01	2.92E-03	**	5.95E-03	2.20E-03	**
	$(\tau = 7)$	1.86E-02	3.02E-03	**	-9.72E-02	2.92E-03	**	1.12E-02	2.21E-03	**
	$(\tau = 8)$	1.54E-02	3.01E-03	**	-9.10E-02	2.92E-03	**	1.43E-02	2.21E-03	**
	$(\tau = 9)$	2.00E-02	3.01E-03	**	-8.50E-02	2.91E-03	**	6.57E-03	2.20E-03	**
	$(\tau = 10)$	1.54E-02	3.00E-03	**	-7.04E-02	2.90E-03	**	9.64E-03	2.19E-03	**
	$(\tau = 11)$	1.53E-02	2.98E-03	**	-6.23E-02	2.89E-03	**	8.35E-03	2.18E-03	**
	$(\tau = 12)$	1.33E-02	2.97E-03	**	-5.82E-02	2.87E-03	**	8.77E-03	2.17E-03	**
	$(\tau = 13)$	9.21E-03	2.96E-03	**	-3.90E-02	2.86E-03	**	8.95E-03	2.17E-03	**
Log Recent	$(\tau = 1)$	2.19E-02	3.91E-03	**	3.02E-02	3.79E-03	**	-1.10E-01	2.86E-03	**
Satisfaction	$(\tau=2)$	2.78E-02	3.94E-03	**	3.10E-02	3.81E-03	**	-1.14E-01	2.88E-03	**
	$(\tau = 3)$	2.61E-02	3.97E-03	**	2.41E-02	3.84E-03	**	-1.11E-01	2.91E-03	**
	$(\tau = 4)$	2.26E-02	4.00E-03	**	2.59E-02	3.87E-03	**	-1.09E-01	2.92E-03	**
	$(\tau = 5)$	2.01E-02	4.01E-03	**	2.33E-02	3.88E-03	**	-1.11E-01	2.94E-03	**
	$(\tau = 6)$	2.20E-02	4.02E-03	**	2.28E-02	3.89E-03	**	-9.93E-02	2.94E-03	**
	$(\tau = 7)$	1.32E-02	4.02E-03	**	2.37E-02	3.89E-03	**	-9.44E-02	2.94E-03	**
	$(\tau = 8)$	2.32E-02	4.02E-03	**	2.29E-02	3.89E-03	**	-8.89E-02	2.94E-03	**
	$(\tau = 9)$	1.46E-02	4.02E-03	**	1.71E-02	3.89E-03	**	-7.96E-02	2.94E-03	**
	$(\tau = 10)$	1.38E-02	4.01E-03	**	2.05E-02	3.88E-03	**	-6.56E-02	2.93E-03	**
	$(\tau = 11)$	8.29E-03	3.99E-03	*	1.50E-02	3.86E-03	**	-5.98E-02	2.92E-03	**
	$(\tau = 12)$	1.90E-02	3.97E-03	**	1.50E-02	3.84E-03	**	-5.51E-02	2.90E-03	**
	$(\tau = 13)$	1.61E-02	3.94E-03	**	1.39E-02	3.82E-03	**	-3.77E-02	2.89E-03	**

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 20: Advertising Parameter Estimate Variation with T_a in All-Controls Perceived Quality Model

Ad Par. S	Spec.	1 Ad Lag	2 Ad Lags	3 Ad Lags	4 Ad Lags	5 Ad Lags	6 Ad Lags	7 Ad Lags
	$(\tau = 0)$	2.33E-05	2.13E-05	2.38E-05	1.89E-05	2.27E-05	2.75E-05	3.47E-05
National	$(\tau = 1)$	7.70E-05 **	6.89E-05 **	6.49E-05 **	7.07E-05 **	6.67E-05 **	6.94E-05 **	7.53E-05 **
Trad.	$(\tau=2)$		4.19E-05 *	2.87E-05	2.36E-05	2.66E-05	2.18E-05	2.49E-05
Ads	$(\tau = 3)$			5.31E-05 *	3.58E-05	3.26E-05	3.66E-05	3.04E-05
	$(\tau = 4)$				8.16E-05 **	6.99E-05 **	6.60E-05 **	7.20E-05 **
	$(\tau = 5)$					4.81E-05 *	3.48E-05	2.98E-05
	$(\tau = 6)$						5.68E-05 **	3.95E-05
	$(\tau = 7)$							8.50E-05 **
	$(\tau = 0)$	2.36E-05	2.35E-05	2.67E-05	2.30E-05	2.50E-05	3.00E-05	3.26E-05
	$(\tau = 1)$	6.80E-05 **	6.61E-05 **	6.74E-05 **	7.03E-05 **	6.54E-05 **	6.62E-05 **	6.73E-05 **
	$(\tau=2)$		-5.79E-06	-1.26E-05	-1.21E-05	-8.57E-06	-1.31E-05	-1.31E-05
Ads	$(\tau = 3)$			4.20E-05	3.40E-05	3.51E-05	3.92E-05	3.72E-05
	$(\tau = 4)$				3.42E-05	2.68E-05	2.74E-05	2.88E-05
	$(\tau = 5)$					3.97E-05	3.18E-05	3.16E-05
	$(\tau = 6)$						4.49E-05	3.91E-05
	$(\tau = 7)$							1.65E-05
	$(\tau = 0)$	2.37E-05	2.42E-05	2.54E-05	2.76E-05	2.89E-05	2.88E-05	2.85E-05
Digital	$(\tau = 1)$	6.64E-05	6.17E-05	6.20E-05	6.08E-05	6.17E-05	6.17E-05	6.21E-05
Ads	$(\tau=2)$		-1.76E-06	-3.59E-05	-3.58E-05	-3.69E-05	-3.65E-05	-3.61E-05
	$(\tau = 3)$			5.00E-05	3.48E-05	3.40E-05	3.27E-05	3.32E-05
	$(\tau = 4)$				8.21E-06	-4.94E-06	-5.32E-06	-6.11E-06
	$(\tau = 5)$					6.46E-06	-3.56E-06	-3.60E-06
	$(\tau = 6)$						-1.20E-06	-1.98E-05
	$(\tau = 7)$							1.80E-05
	$(\tau = 0)$	-3.52E-04	-3.46E-04	-4.24E-04	-4.17E-04	-3.93E-04	-3.77E-04	-3.61E-04
National		-4.52E-04 *	-3.91E-04	-3.97E-04	-4.15E-04	-4.04E-04	-3.91E-04	-3.75E-04
	$(\tau=2)$		-4.12E-04	-3.40E-04	-3.39E-04	-3.43E-04	-3.34E-04	-3.22E-04
	$(\tau = 3)$			-5.27E-04 *	-5.12E-04 *	-4.89E-04 *	-4.95E-04 *	-4.96E-04 *
	$(\tau = 4)$				-9.22E-05	-9.75E-05	-8.88E-05	-7.27E-05
	$(\tau = 5)$					2.10E-05	2.32E-05	1.84E-05
	$(\tau = 6)$						-6.55E-06	-2.74E-05
	$(\tau = 7)$							1.54E-04
	$(\tau = 0)$	1.21E-04	1.40E-04	1.63E-04	1.62E-04	1.35E-04	1.16E-04	1.17E-04
	$(\tau = 1)$	1.51E-04	2.21E-04	2.38E-04	2.25E-04	2.21E-04	2.14E-04	1.99E-04
	$(\tau=2)$		-5.13E-04 *	-5.07E-04 *	-4.96E-04 *	-5.40E-04 *	-5.47E-04 *	-5.49E-04 *
	$(\tau = 3)$			1.57E-04	1.69E-04	1.81E-04	1.79E-04	1.83E-04
	$(\tau = 4)$				-1.41E-04	-1.16E-04	-1.05E-04	-1.09E-04
	$(\tau = 5)$					-3.72E-04	-3.81E-04	-3.76E-04
	$(\tau = 6)$						-8.66E-06	-1.08E-05
	$(\tau = 7)$							-5.48E-05
	$(\tau = 0)$	2.23E-04	2.25E-04	2.15E-04	2.32E-04	1.97E-04	1.30E-04	1.06E-04
	$(\tau = 1)$	4.47E-04	5.36E-04	5.37E-04	5.15E-04	5.25E-04	5.09E-04	4.99E-04
	$(\tau = 2)$		-2.57E-04	-2.27E-04	-2.34E-04	-2.66E-04	-2.62E-04	-2.66E-04
	$(\tau = 3)$			-4.25E-05	9.48E-05	8.08E-05	4.68E-05	4.95E-05
	$(\tau = 4)$				-3.97E-04	-1.37E-04	-1.54E-04	-1.64E-04
	$(\tau = 5)$					-7.89E-04 *	-5.32E-04	-5.40E-04
	$(\tau = 6)$						-7.52E-04 *	-6.91E-04 *
* 00	$(\tau = 7)$							-2.20E-04

^{*} Significant at the 95% confidence level.
** Significant at the 99% confidence level.

Table 21: Ad Parameter Estimates by Industry on Perceived Value

		N	ational Tr	aditonal A	Ads			L	ocal Trad	itional Ac	ls				Digita	al Ads		
	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$
Consumer Goods	-2.15E-04	3.18E-04	-2.35E-04	$2.59\mathrm{E}\text{-}04$	2.21E-05	-2.67E-05	2.05E-04	1.64E-04	2.86E-04	-2.41E-04	9.01E-05	1.16E-04	1.99E-05	-9.05E-05	-1.99E-04	1.28E-04	4.63E-05	-1.99E-04
Tools/Hardware	-4.30E-04	-1.50E-05	-9.13E-05	-4.83E-04	-1.06E-04	-5.29E-05	-5.57E-04	$2.51\mathrm{E}\text{-}04$	-3.53E-04	6.64E-04	$6.74\mathrm{E}\text{-}05$	-4.46E-04	4.27E-04	-3.66E-04	-7.46E-04	$3.67\mathrm{E}\text{-}04$	-1.16E-04	4.56E-04
Soft Drinks	-2.64E-04	9.24E-06	-9.80E-05	$1.30\mathrm{E}\text{-}05$	-1.27E-04	2.97E-04	6.82E-05	$5.23\mathrm{E}\text{-}05$	$3.67\mathrm{E}\text{-}05$	-1.53E-04	-2.62E-04	$3.02\mathrm{E}\text{-}05$	5.61E-04	$1.17\mathrm{E}\text{-}04$	$3.92\mathrm{E}\text{-}04$	-4.70E-04	3.46E-04	$3.31\mathrm{E}\text{-}04$
Beverages: General	1.70E-05	-8.80E-06	$1.45\mathrm{E}\text{-}04$	$2.07\mathrm{E}\text{-}04$	4.78E-05	-8.22E-05	8.25E-05	-6.07E-05	-1.63E-04	-7.67E-05	$6.30\mathrm{E}\text{-}05$	-4.45E-05	-3.14E-04	-8.65E-05	$3.46\mathrm{E}\text{-}04$	$3.07\mathrm{E}\text{-}04$	-1.71E-04	-3.96E-05
Media Devices	-1.25E-04	4.59E-05	-2.79e-04	-6.21E-05	$5.04\mathrm{E}\text{-}05$	-1.96E-04	1.38E-05	$7.29\mathrm{E}\text{-}05$	$8.03\mathrm{E}\text{-}05$	$1.22\mathrm{E}\text{-}05$	$6.34\mathrm{E}\text{-}05$	1.22E-04	1.65E-04	-4.88E-04	$4.41\mathrm{E}\text{-}04$	-2.01E-04	4.69E-04	-8.07E-05
Drugs: OTC	1.50E-04	6.50E-06	-6.38E-05	-1.71E-05	-2.13E-04	2.16E-04	7.56E-05	$2.47\mathrm{E}\text{-}04$	-2.04E-04	7.43E-05	$8.74\mathrm{E}\text{-}05$	-1.52E-06	6.23E-05	$1.04\mathrm{E}\text{-}04$	-9.16E-05	-2.33E-04	8.23E-06	$3.34\mathrm{E}\text{-}05$
Electronics: Audio/Visual	-5.91E-05	-6.26E-05	-2.03E-05	-6.44E-06	2.06E-04	$2.60\mathrm{E}\text{-}05$	1.49E-04	3.56e-04	1.86E-04	$7.09\mathrm{E}\text{-}05$	$6.07\mathrm{E}\text{-}05$	-7.98E-05	8.05E-05	-1.07E-04	2.21E-04	9.44E-05	1.31E-04	-1.72E-04
Internet Sites	3.01E-05	1.57E-04	-2.38E-04	$3.57\mathrm{E}\text{-}05$	-7.77E-05	1.98E-05	-2.69E-04	-2.30E-04	-1.89E-05	1.02E-04	-3.61e-04	1.76E-04	-7.87E-04	-1.42E-04	-3.38E-04	7.30E-04	2.48E-04	-5.08E-04
Home/Furnishing Stores	-3.39E-05	2.39E-04	-1.74E-04	2.60e-04	8.58E-05	3.75E- 05	2.63E-04	1.22E-04	-4.66E-05	9.53E-05	-1.73E-04	3.57E-05	-5.55e-04	-2.09E-04	$1.77\mathrm{E}\text{-}04$	1.07E-04	9.11E-05	$1.31\mathrm{E}\text{-}05$
Appliances	-1.67E-05	1.12E-04	1.69E-04	-3.27E-05	4.07E-05	-2.39e-04	1.48E-04	-4.71E-05	2.22E-04	6.05E-05	5.97E-06	$7.20\mathrm{E}\text{-}05$	2.97E-04	1.20E-04	$4.72\mathrm{E}\text{-}05$	7.98E-05	1.30E-04	3.69E-04
Dept. Stores	1.79E-04	-1.55E-05	3.01e-04	-5.03E-05	-1.35E-04	1.29E-04	1.92E-04	-3.69E-05	6.76 E-05	2.66e-04	-7.94E-05	2.80E-05	2.07E-05	-2.08E-04	1.43E-04	-4.43e-04	1.81E-04	-7.06E-05
Apparel and Shoes	2.89E-06	2.81E-05	-4.54E-05	-9.29E-05	1.80E-04	-5.72E-05	-8.42E-05	5.79E-05	1.53E-04	-1.56E-04	9.50E-05	$2.81\mathrm{E}\text{-}05$	-2.85E-04	1.46E-04	1.96E-04	-9.15E-05	-2.90E-05	1.90E-04
Car Manufacturers	2.26E-04	1.35E-04	2.60E-04	$4.08\mathrm{E}\text{-}04$	-3.44E-04	4.42E-04	-5.59e-04	3.31E-05	-8.13E-05	-2.78E-04	2.10E-04	-8.18E-05	4.69E-04	-2.86E-04	1.88E-04	1.73E-04	-3.44E-04	-7.93E-04
TV Networks	-9.30E-05	-1.56E-05	2.74e-04	-1.76E-05	1.13E-04	-4.46E-05	-3.23E-04	3.67e-04	-2.39E-04	2.50E-04	1.79E-04	-2.44E-04	2.56E-04	-1.52E-04	-4.15E-05	-9.78E-06	7.29E-05	1.31E-04
Hotels	-1.99E-05	1.76e-04	1.77e-04	1.15E-04	2.03e-04	-3.38E-05	-1.71E-04	2.97e-04	5.06E-05	-2.38E-04	-1.57E-04	1.49E-04	-1.28E-04	-2.11E-04	-1.77E-05	3.79E-04	-7.78E-05	3.08E-04
Fast Food	2.15E-04	-6.61E-05	-1.19E-04	1.18E-04	-3.35E-04	-1.17E-04	-1.12E-04	3.73e-04	-2.02E-04	3.17E-04	-7.42E-05	1.36E-04	3.01E-04	-1.16E-04	3.58E-04	-3.36E-04	-1.72E-04	4.52e-04
Liquor	2.48E-05	8.92E-05	1.94E-04	-7.86E-05	2.10E-05	-2.60E-05	9.00E-05	-1.66E-04	2.05E-05	-8.24E-05	-1.86E-04	-1.67E-04	-6.98E-05	-1.92E-04	1.00E-04	3.22E-05	5.63E-05	7.37E-05
Ice Cream/Pizza/Coffee	-2.01E-04	3.95e-04	-1.64E-04	2.56E-04	1.31E-04	-1.59E-05	4.15E-05	-9.50E-05	2.65E-04	-3.60E-05	1.19E-04	3.59E-04	4.67E-04	-4.10E-04	4.38E-04	-6.30E-05	2.49E-04	5.53E-05
Clothing Stores	6.92E-05	-2.68E-06	1.25E-04	-1.83E-04	2.70E-04	1.32E-04	1.15E-04	2.48E-04	1.26E-04	-2.59E-04	4.47E-05	2.69E-04	4.15E-04	7.08E-05	7.30E-05	1.13E-04	-1.67E-04	2.41E-04
Books/Kids/Office Stores	1.55E-04	-2.27E-04	1.22E-04	-1.27E-04	7.67E-05	2.20E-04	3.88E-05	8.66E-05	1.66E-04	1.48E-04	-1.03E-04	1.32E-05	4.61E-05	-3.05E-04	1.57E-04	2.14E-04	-2.20E-04	4.31e-04
Casual Dining	8.39E-05	2.35E-04	-1.10E-04	1.21E-05	-3.47e-04	1.66E-04	1.37E-05	-9.64E-05	6.85E-05	-1.01E-04	8.16E-05	-1.50E-05	-4.71E-05	7.64E-05	1.21E-04	-1.63E-04	-1.19E-04	1.63E-04
Beer	-1.45E-04	-5.97E-05	2.23E-04	-1.44E-05	9.35E-05	2.07E-04	-2.57E-04	1.10E-04	1.22E-04	-8.57E-05	1.37E-04	1.25E-04	-1.44E-04	-1.72E-04	3.24E-04	2.19E-04	-2.01E-04	-1.21E-04
Fast Casual Dining	-8.05E-05	2.85E-04	4.20e-04	-1.24E-04	-2.60E-04	9.24E-05	-1.07E-04	-9.29E-05	-2.43E-04	1.74E-04	-4.09E-05	-5.43E-05	-2.25E-04	-6.14E-05	7.18E-05	-6.00e-04	1.43E-04	1.50E-04
Gasoline/AutoAccessories	-6.45E-05	7.34E-05	6.85E-05	8.32 E-05	-1.34E-06	-3.83E-05	1.60E-04	-7.00E-05	-1.08E-04	1.51E-05	-1.42E-05	6.97E-05	7.32E-06	2.76E-04	-4.92e-04	4.51e-04	-1.49E-04	-3.33E-04
Sports/Electronics Stores	-1.62E-05	4.40E-05	2.64E-04	4.58E-06	-2.21E-04	-2.76e-04	1.55E-04	-3.08e-04	4-4.92E-07	1.00E-05	-1.67E-04	9.37E-05	7.91E-05	1.16E-04	2.64E-05	-7.38E-05	2.50E-04	-3.02E-04
Cruise/TravelAgents	3.01e-04	8.00E-05	8.48E-05	-1.47E-05	-1.06E-05	-1.28E-05	5.02e-04	2.10E-04	1.27E-04	-2.16E-04	-2.52E-05	1.02E-04	3.91E-04	-2.72E-04	-1.75E-04	5.26E-04	-9.73E-05	-1.27E-05
Media Services	1.02E-05	1.31E-04	-8.44E-05	-6.38E-05	-5.23E-05	-2.06E-04	1.59E-04	-2.09E-05	1.47E-04	6.14E-05	-5.54E-05	1.58E-04	1.77E-04	-3.10E-04	5.16E-04	7.31E-05	-3.10E-05	2.50E-04
Insurance	4.07E-05	-5.62E-05	-3.92E-06	9.13E-05	-1.98E-04	1.53E-04	2.60E-04	9.22E-05	-1.29E-04	-2.35E-04	-9.84E-06	-1.09E-04	3.26E-04	-8.57E-05	-1.45E-04	4.39E-04	-3.44E-04	-3.74E-05
Steakhouses/CasualDining	1.59E-04	-2.11E-05	1.04E-04	1.85E-04	-1.03E-04	-1.80E-06	-9.22E-05	9.60E-05	-9.08E-05	4.66E-05	1.01E-04	1.41E-04	1.35E-04	-2.77E-04	2.18E-04	-9.08E-05	3.29E-04	-1.75E-05
Women's Clothing Stores	-3.22E-05	5.35E-05	1.70E-04	-8.04E-05	7.87E-05	8.74E-05	9.81E-05	9.40E-05	6.59E-05	2.51E-04	2.90E-05	-2.06E-05	1.37E-04	-1.32E-04	2.27E-04	1.66E-04	-1.68E-04	1.29E-04
Airlines	3.92E-05	1.68E-04	-7.15E-05	-3.61E-05	1.16E-04	-9.51E-05	-1.02E-04	-1.52E-04	1.07E-04	-1.03E-04	-5.67E-05	1.68E-04	9.04E-05	5.00E-05	2.20E-04	-6.81e-04	4.30E-05	-1.56E-04
Casinos	-3.65E-05	1.37E-05	4.42E-05	-5.69E-05	-6.66E-05	-1.12E-04	-1.09E-04	-7.40E-05	1.66E-04	9.43E-05	-1.12E-04	2.41E-04	-5.21E-04	-1.40E-04	2.11E-04	-5.03E-04	4.94E-04	-2.68E-04
Financial Services	6.18E-05	8.56E-05	1.22E-04	1.30E-04	1.77E-04	6.33E-05	8.33E-05	-9.15E-05	-3.06E-05	-7.52E-05	1.46E-04	7.87E-05	-3.86E-05	-1.55E-04	-1.26E-04	8.42E-05	-1.74E-04	1.67E-05
Grocery Stores	-3.82E-05	8.96E-05	-4.64E-05	-3.18E-04	1.11E-04	-1.02E-04	-9.44E-05	-1.58E-04	-7.49E-05	-4.46E-05	-8.82E-05	1.20E-04	4.73E-05	4.75E-05	2.10E-04	-2.53E-04	9.95E-06	-6.98E-05
Drugs: General	2.11E-04	-1.27E-04	3.02e-04	-7.94E-05	8.48E-05	1.71E-04	2.48E-05	1.60E-04	-8.26E-05	1.55E-04	-9.03E-05	6.15E-05	6.67E-07	-5.04E-05	-2.92E-04	2.74E-04	1.77E-04	-2.11E-04
Drugs: Prescription	9.03E-07	-1.92E-04	-2.53E-06	2.78E-04	-3.51E-05	-2.82E-04	-3.21e-04	4.89E-05	1.25E-05	4.23E-06	2.35E-04	1.53E-04	-2.48E-04	1.92E-04	-3.08E-04	2.88E-04	-3.55E-04	-7.04e-04
Consumer Banks	4.89E-05	-4.44E-06	-8.18E-05	-1.28E-04	1.37E-04	-1.96E-05	1.28E-04	-2.30E-05	-1.50E-04	5.17E-05	7.77E-06	1.17E-05	-7.43E-05	2.96E-04	1.29E-04	-3.89e-04	1.26E-04	6.84E-05

Note: Estimates in bold are statistically significant at the 95% level.

Table 22: Ad Parameter Estimates by Industry on Recent Satisfaction

		N	ational Tr	aditonal A	Ads			I	Local Trad	itional Ad	s				Digita	l Ads		
	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	$\tau = 0$	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$
Consumer Goods	6.15E-05	1.49E-04	1.40E-04	1.10E-04	-1.49E-04	4.61e-04	-1.71E-04	1.52E-04	-3.56e-04	1.67E-04	-7.75E-05	1.42E-04	2.08E-04	1.31E-04	-8.14E-06	1.08E-04	1.86E-04	-1.28E-04
Tools/Hardware	4.53E-04	-1.13E-04	4.99E-05	5.59e-04	-6.70e-04	-5.01E-05	4.72E-04	-2.61E-04	3.14E-04	-2.00E-04	1.73E-05	1.43E-05	-2.30E-04	1.64E-04	3.23E-04	3.11E-04	-1.47e-03	1.31e-03
Soft Drinks	-2.47E-04	1.56E-04	2.14E-05	7.94E-05	6.33E-05	1.99E-04	-1.08E-05	1.32E-04	1.19E-04	-1.06E-04	-1.22E-05	8.95E-05	-1.63E-05	-1.31E-04	3.41E-06	1.67E-04	-2.83E-04	1.58E-04
Beverages: General	-7.95E-05	-1.53E-04	l-1.63E-04	1.92e-04	1.48E-04	-7.35E-05	-9.86E-05	2.89E-05	-1.84E-04	-2.34E-05	4.89E-05	5.75E-05	2.47E-04	6.96E-05	-3.00E-05	-1.45E-04	8.36E-05	6.28E-05
Media Devices	-7.55E-05	8.13E-06	-8.10E-05	1.39E-04	1.14E-04	6.45E-05	-1.27E-04	3.89E-05	-1.23E-04	-1.39E-05	-1.60E-06	3.58E-05	1.33E-04	-1.61E-04	2.58E-04	-1.45E-04	-2.08E-04	3.21E-06
Drugs: OTC	6.70E-05	1.86E-04	1.29E-04	-5.67E-05	3.34E-05	8.78E-05	-1.14E-04	-8.50E-05	-3.02E-04	2.36E-05	-1.54E-04	6.46E-05	-3.54E-04	1.98E-04	1.08E-04	-2.42E-04	2.35E-04	-2.11E-04
Electronics: Audio/Visual	-4.48E-05	2.35E-05	8.52E-05	1.19E-04	5.69E-05	8.00E-06	-1.32E-04	-1.30E-04	-1.64E-05	5.68E-05	2.43e-04	6.78E-05	1.25E-05	-3.10E-05	-1.81E-04	2.44E-04	-3.56E-04	9.64E-05
Internet Sites	1.97E-04	5.92E-05	7.95E-05	2.03E-04	1.72E-05	4.07E-05	-3.47e-04	1.28E-04	1.43E-04	2.24E-04	6.73E-05	-4.86e-04	-3.86E-04	1.04E-04	3.90E-04	-5.21E-05	-7.54e-04	1.03E-04
Home/Furnishing Stores	-1.86E-04	7.22E-05	1.14E-04	-3.78E-05	3.07e-04	1.27E-04	-3.02e-04	-3.75E-05	-6.22E-05	-2.37e-04	-1.07E-05	2.24E-05	1.96E-04	1.62E-04	-5.06E-05	-9.15E-05	2.16E-04	5.67E-05
Appliances	1.32E-04	-6.55E-05	8.09E-05	2.14E-05	-3.60E-05	-2.01e-04	3.94e-04	-9.36E-06	2.29E-05	4.51E-05	9.70E-05	2.50e-04	3.98e-04	-3.62E-04	4.09E-04	1.48E-05	-9.89E-05	-2.18E-04
Dept. Stores	9.55E-05	9.03E-05	-4.34E-05	-8.13E-05	3.21E-05	8.83E-05	-7.68E-05	-1.50E-04	-1.25E-05	6.53E-05	1.08E-04	-4.65E-05	5.85E-05	-1.38E-07	1.72E-04	-1.02E-04	2.65E-05	8.34E-05
Apparel and Shoes	1.52e-04	6.35E-05	1.87E-07	5.60E-05	1.13E-04	7.11E-05	-1.63E-04	2.85E-06	-7.18E-05	-2.32e-04	5.62E-05	-1.41E-04	2.46E-04	-3.64E-05	-1.18E-05	-8.37E-05	-5.50E-05	-1.47E-04
Car Manufacturers	-3.11E-04	1.79E-05	3.09E-04	-2.61E-04	1.65E-04	-3.43e-04	-1.69E-04	5.53E-05	-3.52E-05	7.15E-05	1.67E-04	-1.23E-05	-1.01E-04	1.90E-05	-1.38E-04	-3.22E-04	-7.33E-04	1.89E-05
TV Networks	-5.79E-05	-9.65E-05	1.20E-04	-8.36E-05	-6.64E-05	1.29E-04	-5.73E-06	8.09E-05	1.12E-04	2.01E-04	-2.07E-04	3.94E-05	7.87E-05	3.04E-04	-1.40E-04	3.21E-04	3.91E-06	2.84E-05
Hotels	9.93E-05	3.97E-05	-5.00E-05	4.20E-05	1.77e-04	1.06E-04	1.13E-04	6.98E-05	3.67E-05	4.06E-05	5.15E-05	-4.30E-05	-5.51E-05	1.30E-04	-2.58E-04	-2.98E-04	-6.11E-05	-1.30E-05
Fast Food	2.19E-04	-2.35E-04	1-2.43E-05	2.30E-04	-1.87E-05	-1.71E-04	-1.08E-04	-5.41E-05	2.50E-06	-2.73e-04	-1.29E-04	9.83E-05	-2.80E-04	9.74E-05	-9.11E-06	2.29E-04	-6.38E-05	-2.97E-04
Liquor	6.93E-05	-1.40E-05	1.33E-04	-2.32E-05	2.47e-04	6.35E-05	-3.16E-05	2.71e-04	-7.73E-05	-4.76E-05	-6.70E-07	-1.92E-04	-1.85E-04	6.80E-05	2.66E-04	-2.99E-04	-2.38E-05	8.67E-05
Ice Cream/Pizza/Coffee	-1.37E-05	8.56E-05	2.03E-04	-1.26E-06	-1.23E-04	-9.46E-05	-4.19E-05	-1.35E-04	-9.36E-05	-1.90E-05	7.48E-05	9.93E-05	1.09E-04	-3.13E-05	-1.87E-06	3.43E-04	-2.52E-04	3.53E-04
Clothing Stores	7.71E-05	1.04E-05	3.93E-05	-2.25E-04	9.05E-05	-3.05e-04	1.52 E-05	-4.20E-05	8.33E-05	2.94E-04	1.73E-04	3.35e-04	-1.35E-04	1.55E-04	5.17e-04	-3.64E-04	-2.14E-04	3.09E-04
Books/Kids/Office Stores	1.00E-04	3.03E-05	-3.31E-05	1.90E-06	5.46E-05	-1.76E-05	1.48E-04	-8.88E-05	1.97e-04	-3.13E-05	-9.77E-06	1.52E-04	-9.85E-06	-3.69E-05	1.26E-04	-2.32E-04	2.03E-04	1.06E-04
Casual Dining	-7.61E-05	9.42E-05	-1.98E-04	7.65E-05	-9.47E-05	$8.81\mathrm{E}\text{-}05$	1.11E-04	1.26E-05	1.06E-04	-1.09E-04	-9.47E-05	-1.61E-04	3.81E-05	-9.02E-05	-2.85E-05	1.82E-06	1.24E-04	-3.14E-05
Beer	1.84E-04	3.68E-05	5.37E- 05	1.25E-04	2.98e-04	8.24E-05	3.11E-05	6.52E-05	1.96E-05	9.07E-05	-1.57E-05	1.35E-04	3.85e-04	-4.70e-04	4-4.44E-05	2.23E-05	-1.09E-04	-1.30E-04
Fast Casual Dining	-7.62E-05	-7.14E-05	2.73e -04	-5.95E-05	-3.85E-05	7.31E-05	3.71E-05	-4.23E-06	-1.30E-05	-3.92E-07	4.91E-05	$1.25\mathrm{E}\text{-}04$	1.15E-05	$7.68\mathrm{E}\text{-}06$	-3.34E-04	1.16E-04	-6.13E-05	1.94E-04
Gasoline/AutoAccessories	-2.90E-05	-2.58E-05	5 1.71E-07	7.62E-05	-3.20E-05	-5.13E-05	$2.49\mathrm{e}\text{-}04$	9.74E-05	$8.33\mathrm{E}\text{-}05$	-1.90E-05	-6.87E-05	-1.45E-04	-1.86E-04	-1.40E-05	2.13E-04	-2.36E-04	$3.10\mathrm{E}\text{-}04$	-1.93E-05
Sports/Electronics Stores	-1.08E-04	1.93E-04	2.51E-05	-8.88E-05	$5.22\mathrm{E}\text{-}05$	-4.96E-05	$1.80\mathrm{E}\text{-}04$	1.95E-04	-1.04E-04	$4.97\mathrm{E}\text{-}05$	-1.16E-04	$3.59\mathrm{E}\text{-}05$	-1.26E-04	2.72E-04	-1.30E-04	1.37E-04	1.33E-04	-2.42E-04
Cruise/TravelAgents	9.17E-06	5.31E-05	1.59E-04	2.08e-04	$4.86\hbox{E-}05$	3.33E-05	-2.31E-04	6.08E-06	-8.11E-05	-2.87e-04	-1.48E-05	-1.28E-04	-1.03E-04	$2.10\mathrm{E}\text{-}04$	-1.20E-04	-4.76E-05	4.28E-04	-7.27E-06
Media Services	-1.34E-04	-3.81E-05	5-9.64E-05	1.99E-04	-1.20E-04	-3.04E-05	-1.40E-05	1.02E-04	3.05E-05	$1.60\mathrm{E}\text{-}04$	-1.09E-05	7.81E-05	-3.47E-05	-1.99E-04	7.58E-05	-1.63E-04	$4.32\mathrm{E}\text{-}05$	$4.59\mathrm{E}\text{-}05$
Insurance	-8.90E-05	-1.22E-04	4.95E-05	3.12E-05	$6.17\mathrm{E}\text{-}05$	$2.29\mathrm{e}\text{-}04$	-2.89E-05	1.28E-05	7.71E-05	-1.03E-05	-8.88E-06	$3.40\mathrm{E}\text{-}05$	-2.92E-04	4.91e-04	-6.20E-05	-1.52E-04	-4.69E-06	-2.08E-04
Steakhouses/CasualDining	6.74E-05	1.86E-05	-1.63E-04	2.92E-05	-9.24E-05	-1.26E-04	-5.62E-05	1.20E-05	-1.56E-04	-4.49E-05	-1.61E-04	$8.18\mathrm{E}\text{-}05$	-2.79E-04	4.19e-04	-1.35E-05	3.36E-05	$3.81\mathrm{E}\text{-}05$	-2.16E-04
Women's Clothing Stores	-1.10E-05	1.73E-04	-7.81E-05	3.62E-05	-1.68E-04	2.11E-06	2.13E-04	-5.63E-05	$6.80\mathrm{E}\text{-}05$	-1.19E-04	7.94E-05	8.43E-05	2.10E-04	$1.37\mathrm{E}\text{-}05$	-2.33E-04	6.46E-05	$3.00\mathrm{E}\text{-}05$	-1.07E-04
Airlines	1.09E-04	-9.65E-05	51.44e-04	7.34E-05	-1.15E-04	-1.08E-04	-8.26E-05	1.68E-05	-8.40E-06	$2.59\mathrm{E}\text{-}05$	-2.87E-05	$1.74\mathrm{E}\text{-}05$	-6.73E-05	4.82E-05	-1.87E-04	1.81E-06	$4.26\hbox{E-}05$	3.93E-05
Casinos	-3.86E-05	-8.35E-05	6.52E-05	2.18E-05	-4.45E-05	-7.52E-07	-1.96E-04	5.69E-05	$9.81\mathrm{E}\text{-}05$	1.36E-04	-5.75E-05	-9.55E-05	9.88E-05	-1.47E-04	-6.41E-06	3.98E-04	$2.68\mathrm{E}\text{-}04$	-2.79E-04
Financial Services	-3.07E-06	2.70E-06	$1.19\mathrm{E}\text{-}04$	2.81E-05	-2.91E-05	-5.00E-05	$2.96\mathrm{E}\text{-}05$	4.96E-06	-4.44E-05	-4.01E-06	-5.33E-05	-5.39E-06	3.10E-05	-7.65E-05	-1.91E-04	2.16E-04	-1.51E-04	-1.03E-04
Grocery Stores	-2.32E-05	-1.40E-04	1.57E-04	-8.79E-05	-5.73E-06	-5.90E-05	-1.86E-04	5.28E-05	-2.71E-05	1.53E-04	-8.67E-05	-2.48E-05	-3.81E-05	7.45E-05	-7.99E-05	3.38e-04	-1.67E-04	-6.57E-06
Drugs: General	4.04E-05	-5.19E-05	1.54e- 04	1.69E-05	5.51E-05	3.25E-06	-1.39E-04	2.58E-05	-1.44E-04	-7.20E-05	-1.18E-04	$3.78\mathrm{E}\text{-}05$	-1.44E-04	2.10E-04	-1.84E-04	6.39E-05	-1.28E-04	1.03E-04
Drugs: Prescription	-4.71E-05	-5.72E-05	6-6.64E-05	-1.22E-04	1.13E-04	1.49E-04	-4.76E-05	1.39E-04	2.29E-05	4.03E-05	-5.59E-05	-5.00E-05	-2.83E-04	-3.34E-04	5.05e-04	7.66E-05	$1.29\mathrm{E}\text{-}05$	8.67E-05
Consumer Banks	4.13E-05	5.09E-05	-6.92E-05	6.59E-06	9.64E-05	-1.38E-04	4.65E-05	2.48E-05	9.21E-05	$5.72\mathrm{E}\text{-}05$	-9.09E-05	1.24E-04	-2.75E-05	-1.34E-05	-1.83E-04	1.98E-04	-2.01E-04	1.90E-04

Note: Estimates in bold are statistically significant at the 95% level.

Table 23: All-controls model estimated using 2-week data aggregation

Brand Attitude Models		Perceived Quality			Perceived Value			Recent Satisfaction		
		Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Own Nat'l	$(\tau = 0)$	6.86E-05	2.31E-05	**	8.29E-05	2.21E-05	**	2.03E-05	1.65E-05	
Trad. Ads	$(\tau = 1)$	7.49E-05	2.30E-05	**	9.17E-05	2.20E-05	**	7.30E-05	1.64E-05	**
	$(\tau=2)$	9.76E-05	2.30E-05	**	5.07E-05	2.20E-05	*	4.47E-05	1.64E-05	**
Own Loc.	$(\tau = 0)$	4.03E-05	2.71E-05		6.20E-05	2.60E-05	*	-1.04E-05	1.93E-05	
Trad. Ads	$(\tau = 1)$	7.63E-05	2.72E-05	**	3.11E-05	2.61E-05		-1.40E-05	1.94E-05	
	$(\tau = 2)$	3.55E-05	2.70E-05		2.45E-05	2.58E-05		-2.32E-06	1.92 E-05	
Own Dig.	$(\tau = 0)$	4.36E-05	3.68E-05		-2.97E-05	$3.53\mathrm{E}\text{-}05$		-1.34E-06	$2.62\mathrm{E}\text{-}05$	
Ads	$(\tau = 1)$	4.33E-05	3.84E-05		5.59E-07	3.67E-05		5.94E-05	2.73E-05	*
	$(\tau=2)$	5.51E-05	$3.66\hbox{E-}05$		3.93E-05	3.51E-05		-3.00E-05	2.61E-05	
Comp. Nat'l	$(\tau = 0)$	-7.43E-04	2.93E-04	*	-4.27E-04	2.81E-04		-7.95E-05	2.09E-04	
Trad. Ads	$(\tau = 1)$	-9.50E-04	$2.90\hbox{E-}04$	**	-1.08E-03	2.78E-04	**	-6.67E-05	2.07E-04	
	$(\tau=2)$	-3.29E-04	$2.85\hbox{E-}04$		-5.49E-04	2.73E-04	*	1.10E-04	2.03E-04	
Comp. Loc.	$(\tau = 0)$	2.96E-04	2.72E-04		-1.21E-04	$2.60\hbox{E-}04$		-1.09E-04	1.93E-04	
Trad. Ads	$(\tau = 1)$	2.76E-04	2.77E-04		-2.59E-04	2.66E-04		3.55E-05	1.97E-04	
	$(\tau = 2)$	-4.29E-05	2.80E-04		1.60E-04	2.68E-04		-1.88E-04	1.99E-04	
Comp. Dig.	$(\tau = 0)$	4.56E-04	3.74E-04		-5.92E-04	3.58E-04		-3.01E-05	2.66E-04	
Ads	$(\tau = 1)$	1.95E-04	$3.73\mathrm{E}\text{-}04$		-2.42E-04	$3.57\mathrm{E}\text{-}04$		1.86E-04	2.65E-04	
	$(\tau = 2)$	-5.91E-04	3.70 E-04		7.94E-04	3.54E-04	*	-8.60E-04	2.63E-04	**
Perceived	$(\tau = 1)$	-1.84E-01	4.25E-03	**	4.61E-02	4.07E-03	**	2.11E-02	3.03E-03	**
Quality	$(\tau = 2)$	-2.04E-01	4.31E-03	**	3.43E-02	4.12E-03	**	2.13E-02	$3.07\mathrm{E}\text{-}03$	**
	$(\tau = 3)$	-1.87E-01	4.36E-03	**	3.88E-02	4.17E-03	**	2.34E-02	$3.10\hbox{E-}03$	**
	$(\tau = 4)$	-1.58E-01	$4.37\hbox{E-}03$	**	2.47E-02	$4.18\hbox{E-}03$	**	1.43E-02	3.11E-03	**
	$(\tau = 5)$	-1.22E-01	$4.33\hbox{E-}03$	**	2.49E-02	$4.14\hbox{E-}03$	**	1.58E-02	3.08E-03	**
	$(\tau = 6)$	-8.49E-02	$4.28\hbox{E-}03$	**	1.81E-02	$4.10\hbox{E-}03$	**	1.41E-02	3.05E-03	**
Perceived	$(\tau = 1)$	3.57E-02	$4.45\hbox{E-}03$	**	-2.03E-01	$4.25\hbox{E-}03$	**	2.66E-02	3.17E-03	**
Value	$(\tau=2)$	4.56E-02	$4.50\hbox{E-}03$	**	-2.12E-01	$4.30\hbox{E-}03$	**	2.11E-02	$3.20\hbox{E-}03$	**
	$(\tau = 3)$	3.38E-02	4.54E-03	**	-1.97E-01	4.34E-03	**	1.68E-02	3.23E-03	**
	$(\tau = 4)$	3.07E-02	$4.54\hbox{E-}03$	**	-1.69E-01	$4.34\hbox{E-}03$	**	2.36E-02	3.23E-03	**
	$(\tau = 5)$	2.61E-02	$4.49\mathrm{E}\text{-}03$	**	-1.35E-01	$4.29\hbox{E-}03$	**	1.45E-02	$3.19\mathrm{E}\text{-}03$	**
	$(\tau = 6)$	2.00E-02	4.43E-03	**	-9.80E-02	$4.24\hbox{E-}03$	**	1.61E-02	3.16E-03	**
Recent	$(\tau = 1)$	5.06E-02	$6.00\hbox{E-}03$	**	5.18E-02	5.74E-03	**	-2.15E-01	$4.27\hbox{E-}03$	**
Satisfaction	$(\tau=2)$	4.09E-02	6.13E-03	**	4.34E-02	$5.87\mathrm{E}\text{-}03$	**	-2.05E-01	4.37E-03	**
	$(\tau = 3)$	3.72E-02	$6.18\hbox{E-}03$	**	4.36E-02	$5.91\mathrm{E}\text{-}03$	**	-1.94E-01	$4.40\hbox{E-}03$	**
	$(\tau = 4)$	3.57E-02	6.18E-03	**	3.98E-02	5.91E-03	**	-1.65E-01	4.40E-03	**
	$(\tau = 5)$	2.31E-02	6.14E-03	**	3.15E-02	5.87E-03	**	-1.28E-01	4.37E-03	**
	$(\tau = 6)$	3.58E-02	6.03E-03	**	2.69E-02	5.77E-03	**	-9.50E-02	4.29E-03	**

^{*} Significant at the 95% confidence level.

^{**} Significant at the 99% confidence level.

Table 24: All-controls model estimated using 4-week data aggregation

Brand Attitude Models	Perceived Quality			Perceived Value			Recent Satisfaction		
	Est.	Std.Err.		Est.	Std.Err.		Est.	Std.Err.	
Own Nat'l Trad. Ads	9.30E-05	2.94E-05	**	7.13E-05	2.80E-05	*	4.74E-05	2.06E-05	*
Own Loc. Trad. Ads	1.72E-06	3.91E-05		2.42E-05	$3.72\mathrm{E}\text{-}05$		-3.01E-05	$2.73\mathrm{E}\text{-}05$	
Own Dig. Ads	7.69E-05	$3.85\mathrm{E}\text{-}05$	*	7.75E-06	$3.66\mathrm{E}\text{-}05$		3.13E-05	$2.69\mathrm{E}\text{-}05$	
Comp. Nat'l Trad. Ads	-1.14E-03	5.56E-04	*	-1.07E-03	5.29E-04	*	2.51E-04	3.88E-04	
Comp. Loc. Trad. Ads	-7.70E-04	4.38E-04		-5.10E-04	$4.16\hbox{E-}04$		-1.90E-04	$3.06\hbox{E-}04$	
Comp. Dig. Ads	4.04E-04	4.61E-04		-1.09E-03	$4.38\hbox{E-}04$	*	1.70E-04	3.22E-04	
Perceived $(\tau = 1)$	-3.76E-01	6.78E-03	**	5.64E-02	6.45E-03	**	3.69E-02	4.73E-03	**
Quality $(\tau = 2)$	-3.04E-01	6.99E-03	**	4.38E-02	$6.64 \hbox{E-}03$	**	2.86E-02	$4.88\mathrm{E}\text{-}03$	**
$(\tau = 3)$	-1.68E-01	6.80E-03	**	3.65E-02	$6.46\hbox{E-}03$	**	3.09E-02	$4.74\mathrm{E}\text{-}03$	**
Perceived $(\tau = 1)$	6.98E-02	7.05E-03	**	-3.86E-01	$6.70\hbox{E-}03$	**	3.66E-02	4.92E-03	**
Value $(\tau = 2)$	5.60E-02	7.22E-03	**	-3.15E-01	$6.87\mathrm{E}\text{-}03$	**	3.81E-02	5.04E-03	**
$(\tau = 3)$	3.32E-02	7.07E-03	**	-1.89E-01	$6.72 \hbox{E-}03$	**	3.30E-02	4.93E-03	**
Recent $(\tau = 1)$	7.37E-02	9.68E-03	**	8.15E-02	9.21E-03	**	-3.82E-01	$6.76\mathrm{E}\text{-}03$	**
Satisfaction $(\tau = 2)$	5.78E-02	9.93E-03	**	8.10E-02	$9.45\hbox{E-}03$	**	-3.03E-01	6.94E-03	**
$(\tau = 3)$	5.62E-02	9.67E-03	**	5.57E-02	9.19E-03	**	-1.64E-01	6.75E-03	**

^{*} Significant at the 95% confidence level.

^{**} Significant at the 99% confidence level.